



From sensor tips to state and parameter estimates

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Control and Real-time Optimisation
of Intensive Polymerisation

FP7-NMP-2011-Small-5 Grant Agreement 280827

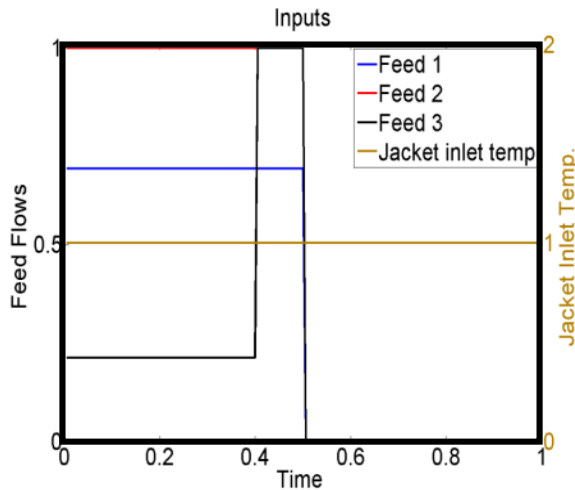


- Motivation: Recipe-based process operation and its drawbacks
- State-based operation.
- State estimation and observability
- Parameter estimation and identifiability
- Raman spectra to concentration and particle sizes.
- Summary

Recipe-based Operation

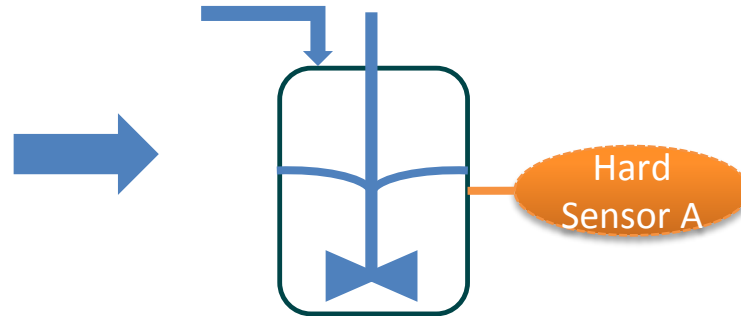
- Current industrial practice.

- Fixed recipe



- Operation based on heuristics and experience.

- Process monitoring using few sensors



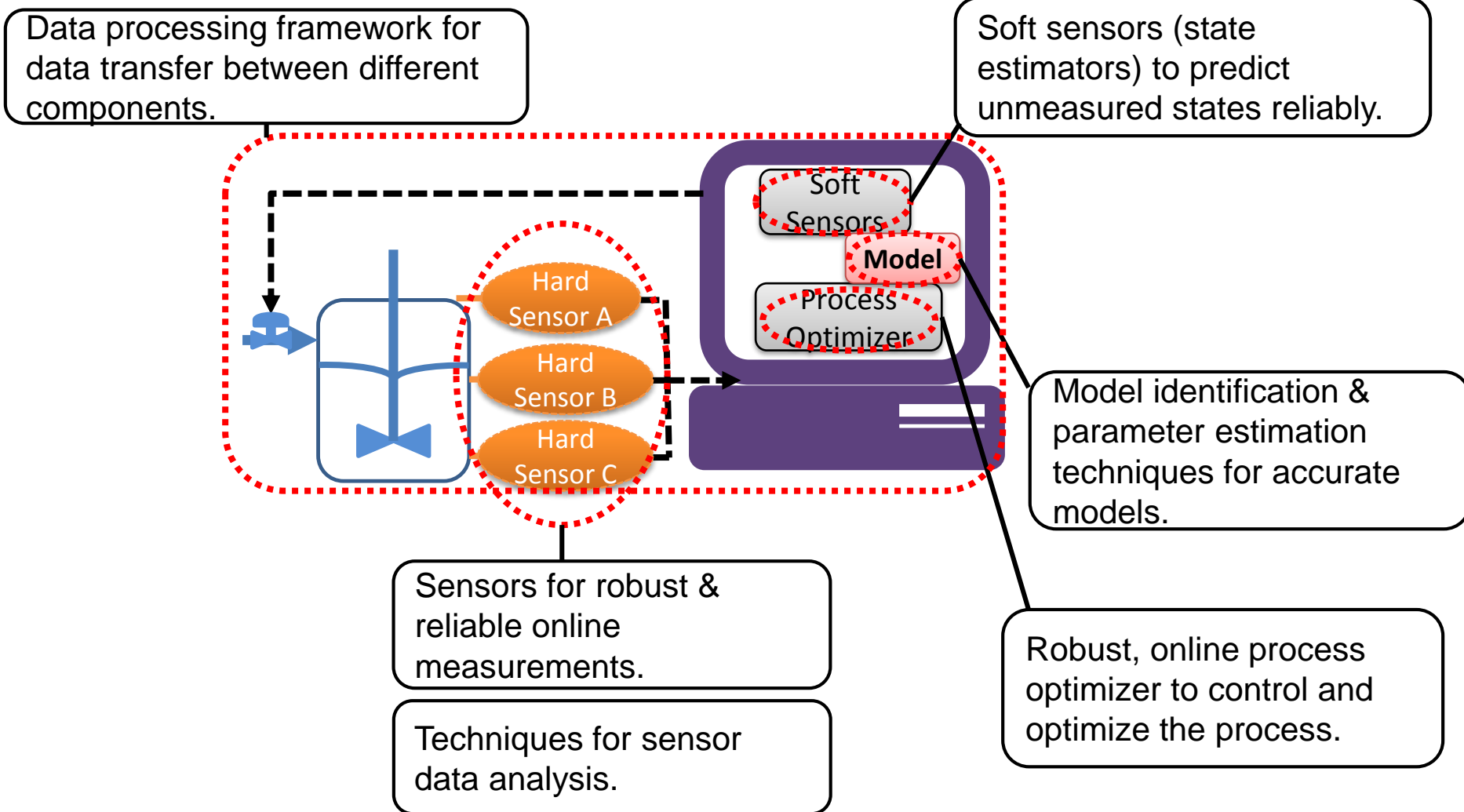
Drawbacks of time-based operation:

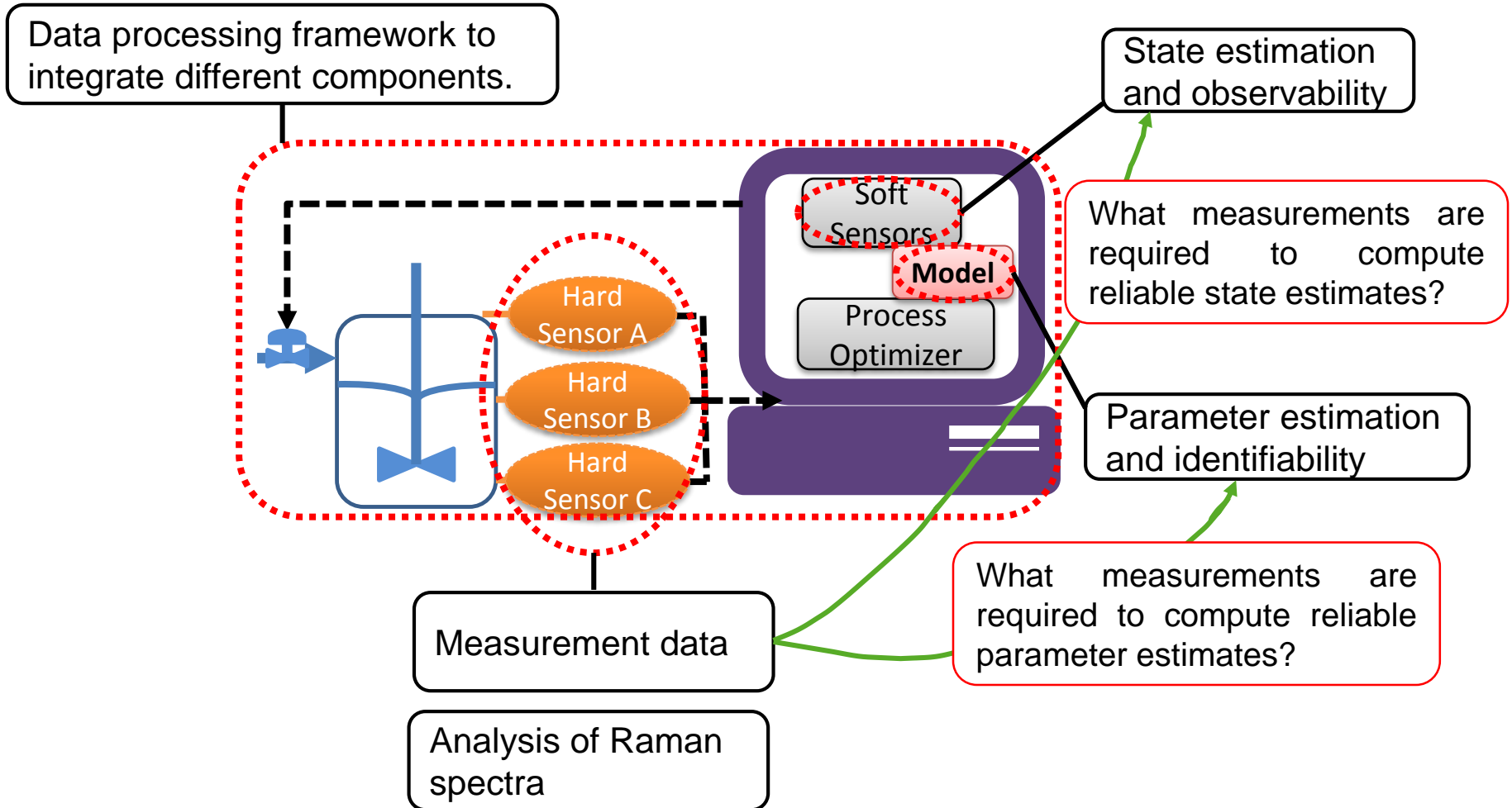
- ✗ Susceptibility to process disturbances.
- ✗ Online process optimization not possible.

Can be solved by

Model-based control/
State-based operation

State-based Operation



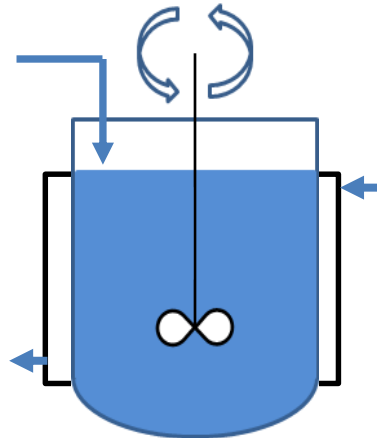


Considered Case Study

4 Monomer semi-batch emulsion polymerization.

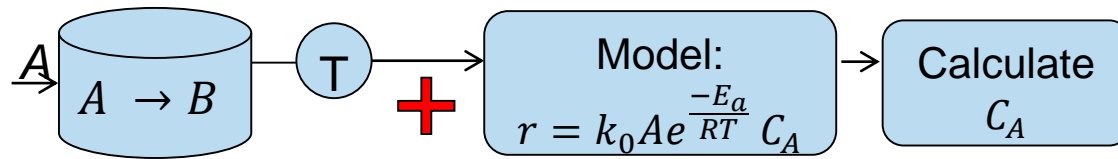
Model

- 48 Differential equations
- ~300 Algebraic equations
- Mass transfer
- Kinetics of monomer conversion
- Kinetics of polymer chain growth
- Heat transfer



Possible Measurements

- Reactor temperature
- Coolant inlet temperature
- Coolant outlet temperature
- Enthalpy of reaction
- Monomer conversions
- No. Avg. Molecular weight (MN)
- Wt. Avg. Molecular weight (MW)

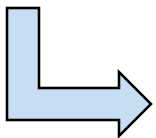


State estimation algorithms: Extended Kalman Filter (EKF)

Moving Horizon Estimators (MHE)

Particle Filters

Challenge in polymerization systems: Is it possible to estimate all the states with available measurement data?



Observability:

- Can all states be estimated?
- Which measurements are required to ensure complete state observability?

Observability Analysis in Case Study

- Definition: A state is said to be observable if it can be uniquely determined from measurements in a finite time¹.
- The semi-batch emulsion polymerization system has a high degree of nonlinearity → A nonlinear observability analysis should be performed.
- Nonlinear observability methods not yet tractable for large scale processes.
- Linear observability analysis performed on models linearized at multiple time points.
- Case I: Observability analysis with measurements
 - Reactor temperature
 - Coolant inlet temperature
 - Coolant outlet temperature
 - Enthalpy of reaction
 - Monomer conversions
 - No. Avg. Molecular weight
 - Wt. Avg. Molecular weight

All states are observable!

¹Kalman, R. E., On the general theory of control systems, *Proc. First IFAC Congress Automatic Control, Moscow*, 1:481-492,1959

Are all measurements available online?

Measurements	Commonly used Analysis techniques	Analysis time*
MN, MW	GPC	40 min
Monomer Conversions	GC, HPLC	25 min

* Does not include time for sample preparation

MN, MW, Monomer conversion require significantly long analysis times!

→ Cannot be used for online estimation.

Observability analysis with online measurements

- Reactor temperature
- Coolant inlet temperature
- Coolant outlet temperature
- Enthalpy of reaction

Not all states are observable!

States in a semi-batch emulsion polymerization model

Subsystem I

States related to material and energy balance, e.g.

- Moles of unreacted monomer
- Reactor temp.

Subsystem II

States related to molecular properties of polymer, e.g.

- Moments of molecular weight



Observable only if online polymer property measurements are available^{1,2}.

Also shown by our observability analysis.

¹Kozub D. J., Macgregor J. F., *Chemical Engineering Science*, 47 (5): 1047-1062, 1992.

²Schuler H., and Suzhen Z., *Chemical Engineering Science*, 40(10): 1891-1904, 1985.

Observability of Material and Energy Balance

Case II: Observability of only material and energy balance equations tested with reduced model and measurements:

- Reactor temperature
- Coolant inlet temperature
- Coolant outlet temperature
- Enthalpy of reaction

Not all states are observable!

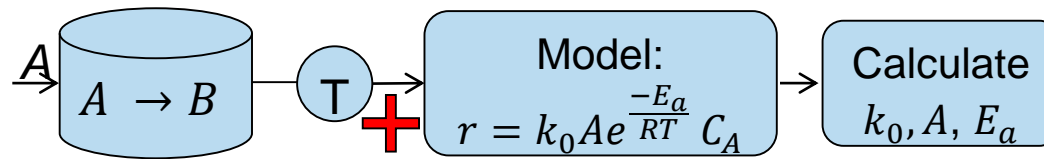
Case III: Material and energy balance with measurements:

- Reactor temperature
- Coolant inlet temperature
- Coolant outlet temperature
- Enthalpy of reaction
- Monomer conversions

All states are observable!



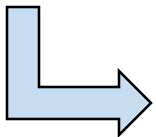
Monomer conversion
estimation of material



Parameter estimation algorithms: Weighted Least Squares
Maximum Likelihood Estimation } Offline methods

Parameter estimation may also be carried out online using with state estimation algorithms (e.g. EKF)

Challenge in polymerization systems: Is it possible to estimate all the parameters with available measurable data?

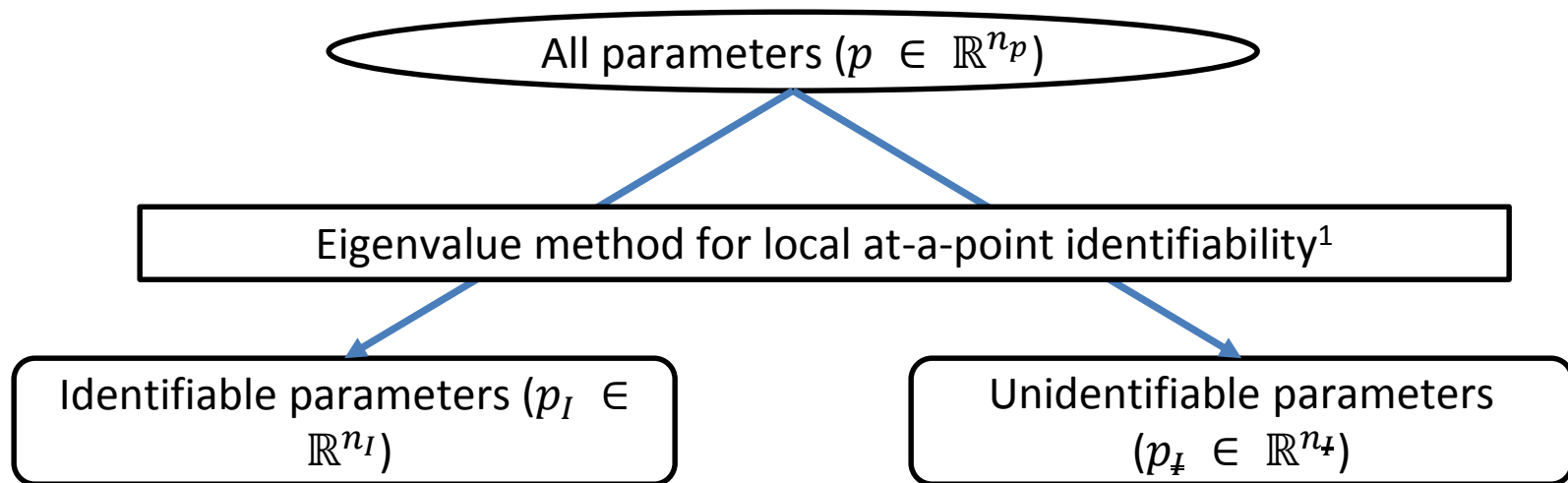


Identifiability:

- Can parameters be uniquely determined from available measurements?

Identifiability Analysis- Definition and Method

- Identifiability definition: A parameter is said to be identifiable if it can be uniquely determined from available measurement and input data.
- Several methods exist to check parameter identifiability. However, only local, at-a-point methods are tractable for large scale systems.



¹Quaiser, T., Data- and model-based identification of biochemical processes, *PhD Thesis*, Ruhr-Universität Bochum, 2011

Identifiability Analysis in Case Study

Identifiability Analysis with measurements

- Reactor temperature
- Coolant inlet temperature
- Coolant outlet temperature
- Enthalpy of reaction **+** ▪ Monomer conversions

Type	Parameter
Mass transfer	$K_{MW_S}, K_{MW_B}, K_{MW_{AA}}, K_{MW_{AAm}}, K_{WP_S}, K_{WP_B}, K_{WP_{AA}}, K_{WP_{AAm}}, V_{kd_1}, V_{kd_2}, V_{kd_3}, V_{kd_4}, V_{kp_1}, V_{kp_2}, k_{abs}, k_{des}$
Reaction Kinetics	$k_{I0}, k_{intra0}, E_{intra}, k_{p1ter0}, E_{p1ter}, k_{p2ter0}, E_{p2ter}, k_{p3ter0}, E_{p3ter}, k_{p4ter0}, E_{p4ter}, a_S, a_B, k_{p0_3}, k_{p0_4}, r_{12}, r_{13}, r_{14}, r_{21}, r_{23}, r_{24}, r_{31}, r_{32}, r_{34}, r_{41}, r_{42}, r_{43}, k_{t0_3}, k_{t0_4}, k_{f0_1}, k_{f0_2}, k_{f0_3}, E_{f_3}, k_{f0_4}, E_{f_4}$
Heat transfer	kA, kA_{v1}, kA_{v2}

Number of identifiable parameters is **19** out of 54

Parameter Estimation – Solution to Suboptimal Estimates

Parameter estimation is typically multimodal optimization problem.

Reasons for model-experiment mismatch:

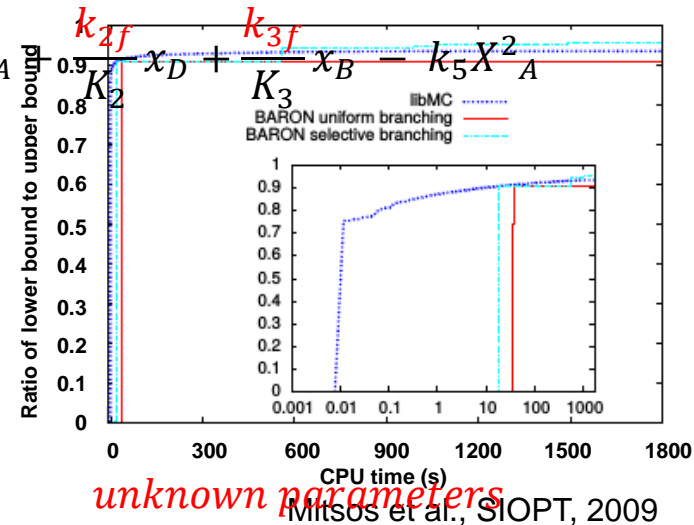
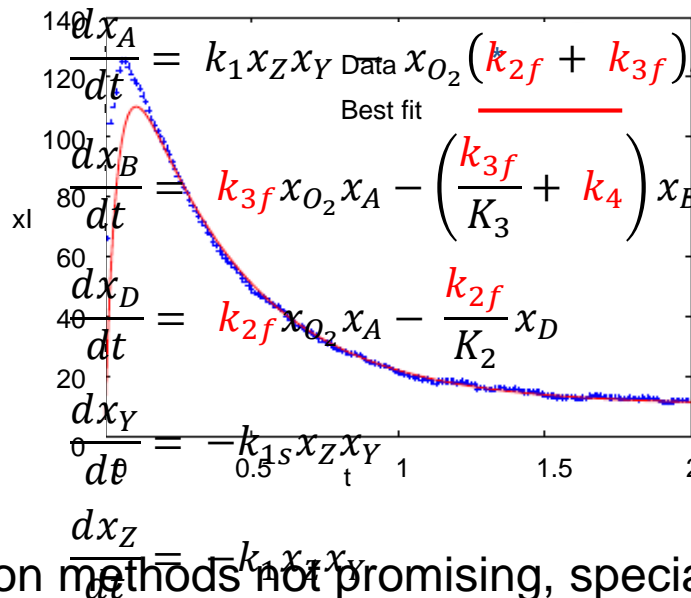
- Wrong experimental data.
- Wrong model structure.
- Suboptimal estimation. → Can be solved through deterministic global optimization.

Case study:

- batch reaction
- 6 states
- 3 unknown parameters: (k_{2f}, k_{3f}, k_4)

xl (Measurements):

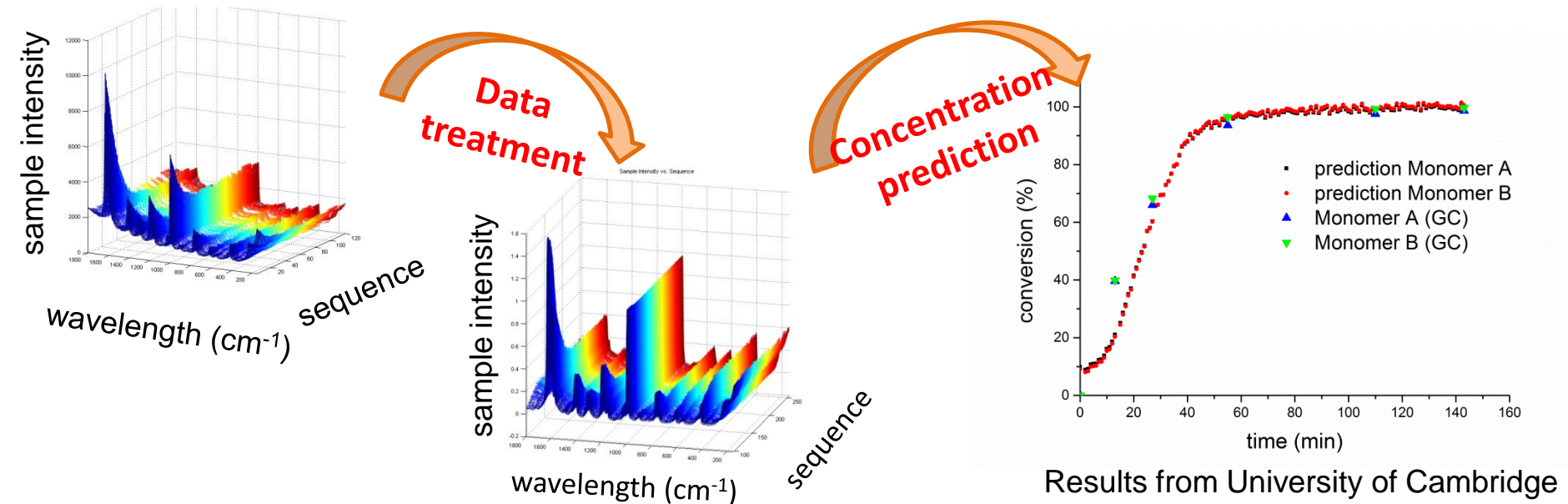
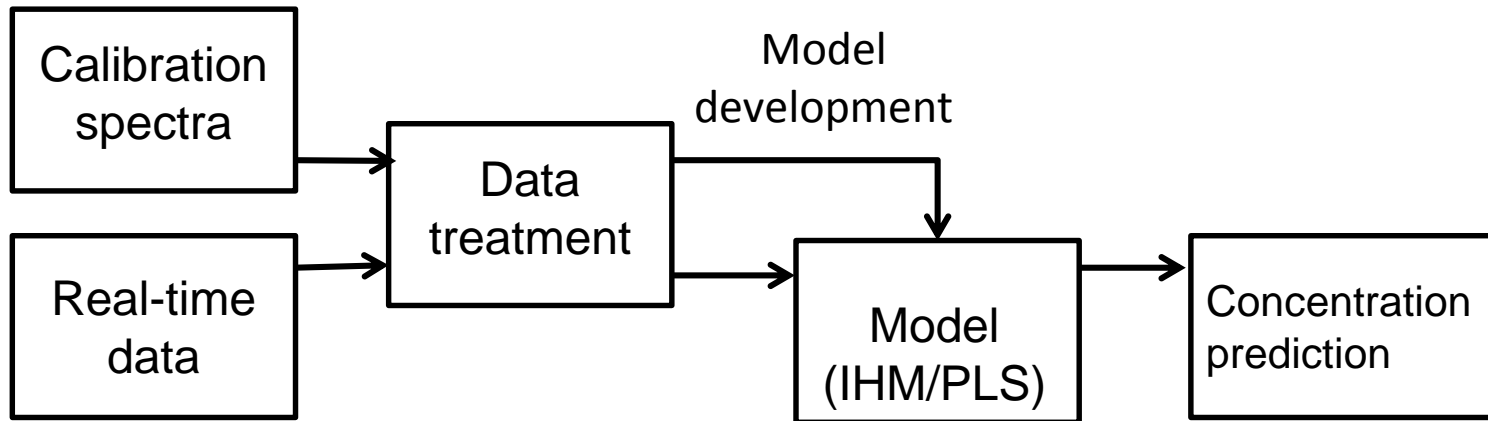
$$x_I = x_A + \frac{2}{21}x_B + \frac{2}{21}x_D$$



Standard optimization methods not promising, specialized ones tractable.

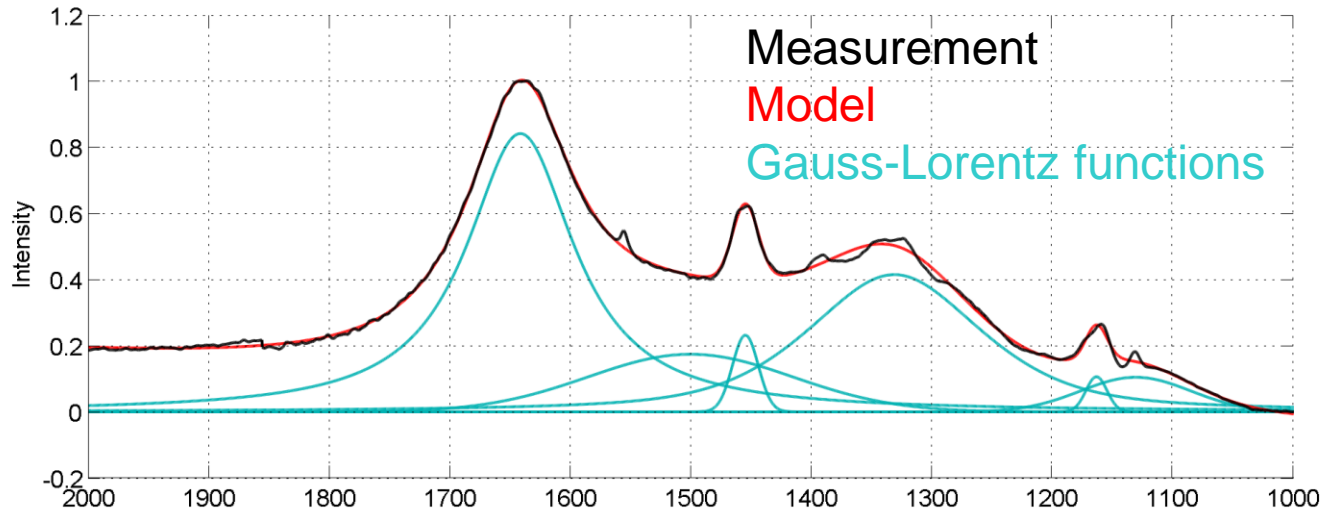
Challenge holds also for other optimization problems, e.g. offline and online optimization.

Raman Spectra → Conversion Prediction (Batch process)



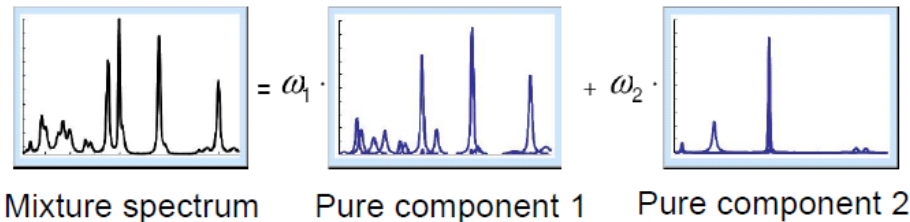
Indirect Hard Modeling¹ (IHM)

Model Raman Spectra of reaction components using Gauss – Lorentz functions.



A model of the mixture (A) is created as weighted sum of the pure component models (A'_k)

$$A(\tilde{\nu}, x) = \sum_{k=1}^K \omega_k(x) A'_k(\tilde{\nu})$$



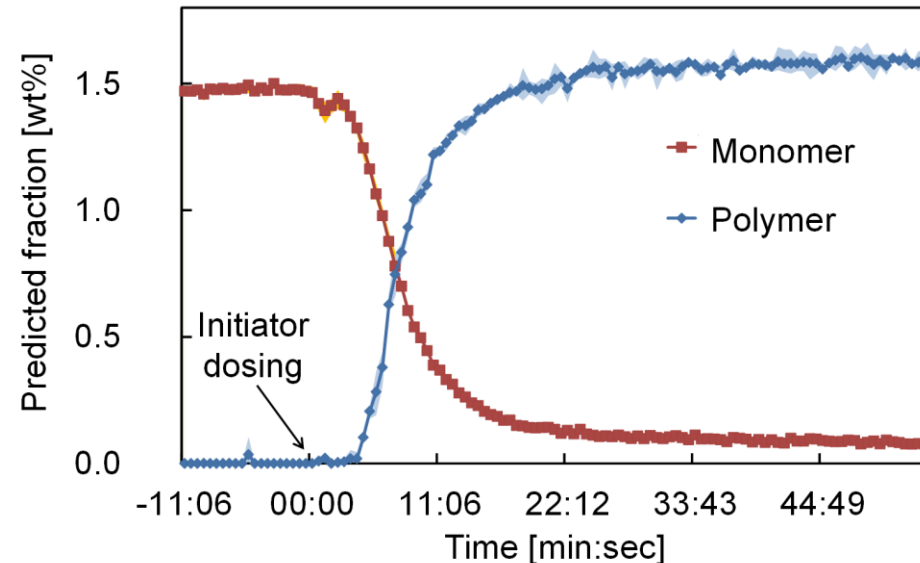
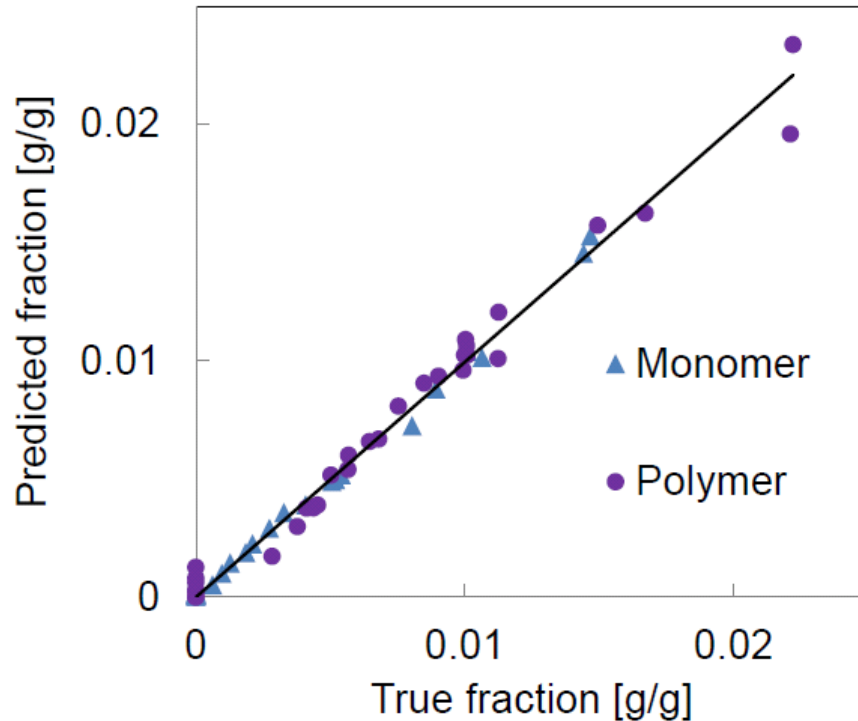
¹Alsmeyer, F., Koß, H.-J., Marquardt, W., *Journal of Applied Spectroscopy*, 58,975-985,2004.

Concentration Estimation from Raman Spectra (Batch Process)



Models calibrated using multivariate regression in PEAXACT¹ software.

Calibrated models are then used for concentration estimation



Monomer RMSECV=0.00028 $R^2=0.9967$
Polymer RMSECV=0.00084 $R^2=0.9835$

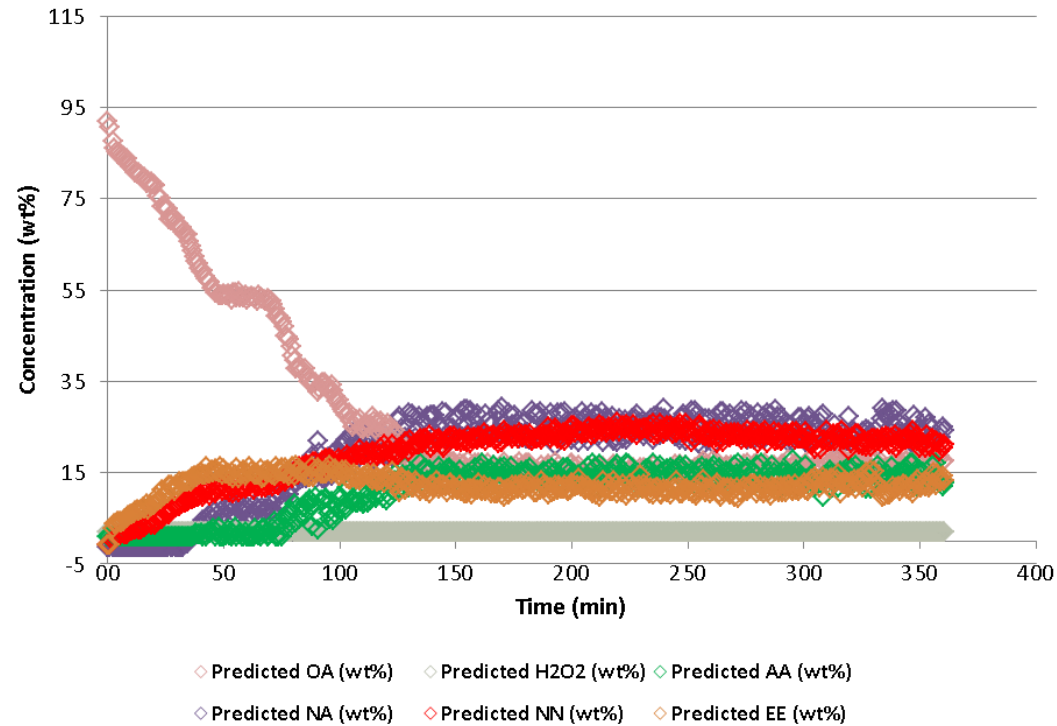
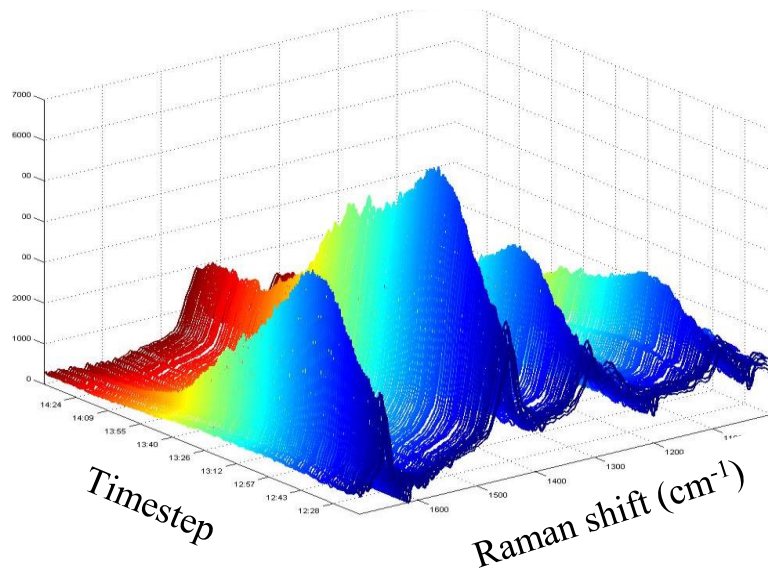
¹PEAXACT, S-PACT GmbH

Julian Meyer-Kirschner, M.Sc



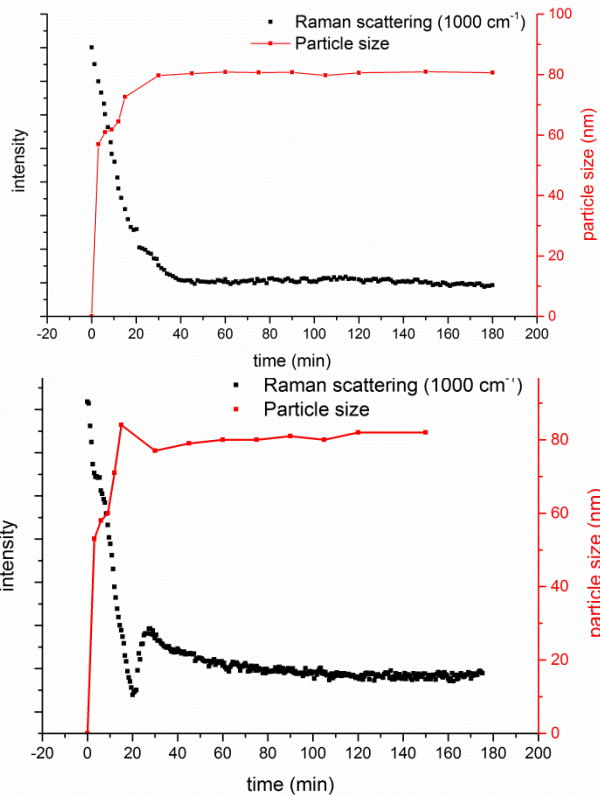
SFB 985
Funktionelle Mikrogele und
Mikrogelsysteme

Monitoring Oxidation of Oleic Acid using Raman Spectra (Batch Process)



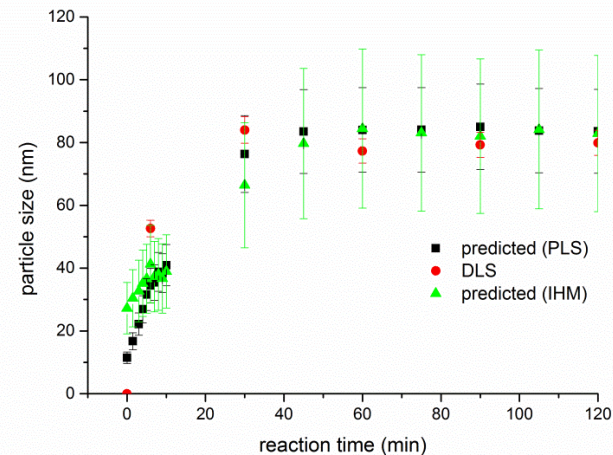
EU Project - OPTICO

Raman Spectra → Particle Size Prediction (Batch Process)



Comparison of particle size (red) and intensity profile (black) during experiments.

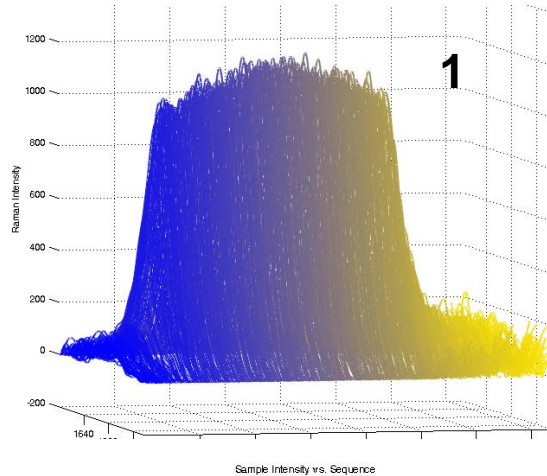
- Model for prediction of particle size is trained on the intensity change at 1000 cm^{-1} .
- Model shows good agreement to offline particle measurement (DLS).



Comparison particle size of PLS, IHM and offline measured with DLS.

Results from University of Cambridge

Raman Spectra → Conversion and Particle Size (Semi-batch Process)

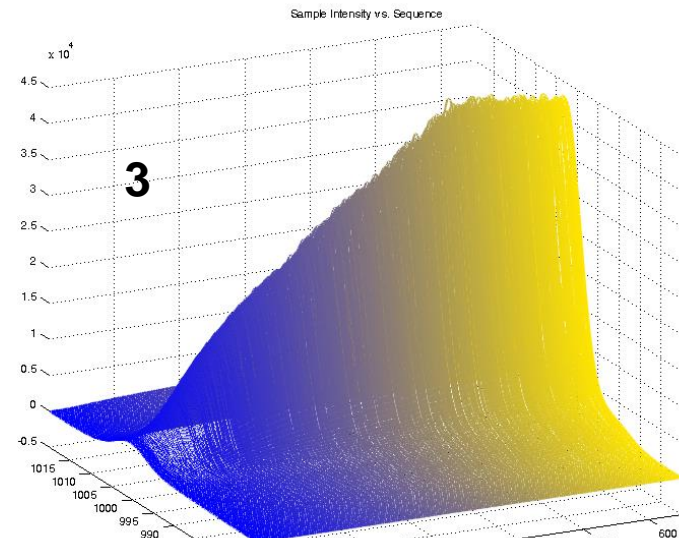
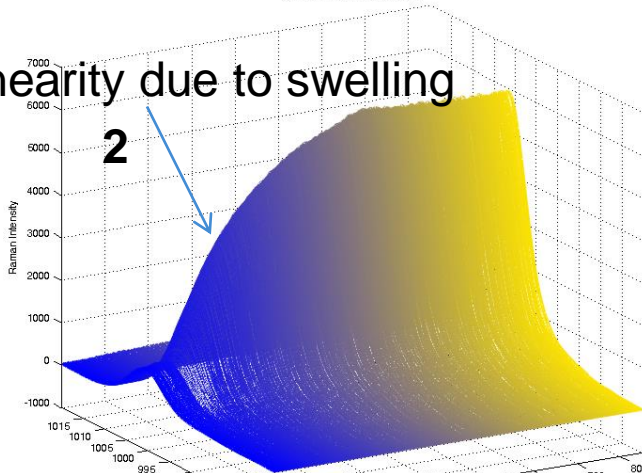


1 Raman intensity for the double bond of styrene under starved conditions

2 Raman intensity for the aromatic ring of styrene under starved conditions

3 Raman intensity for the aromatic ring of styrene without reaction.

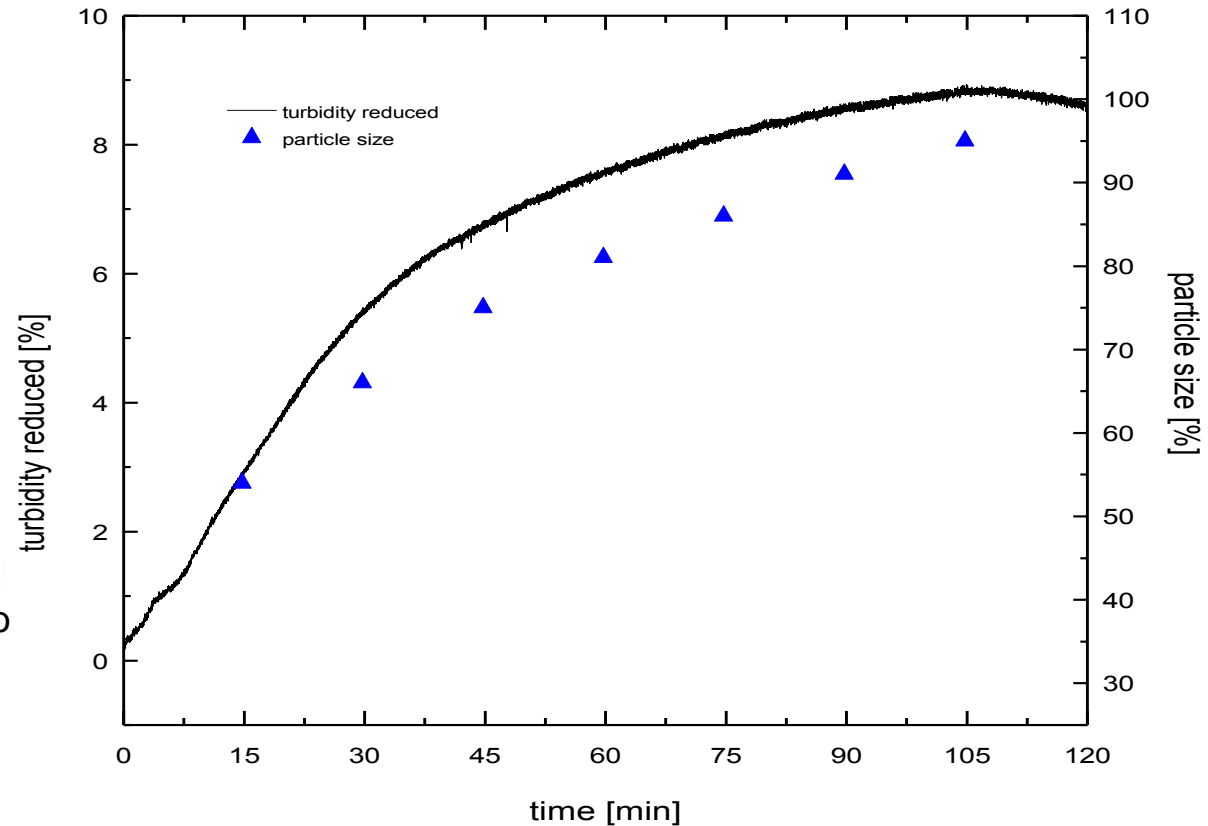
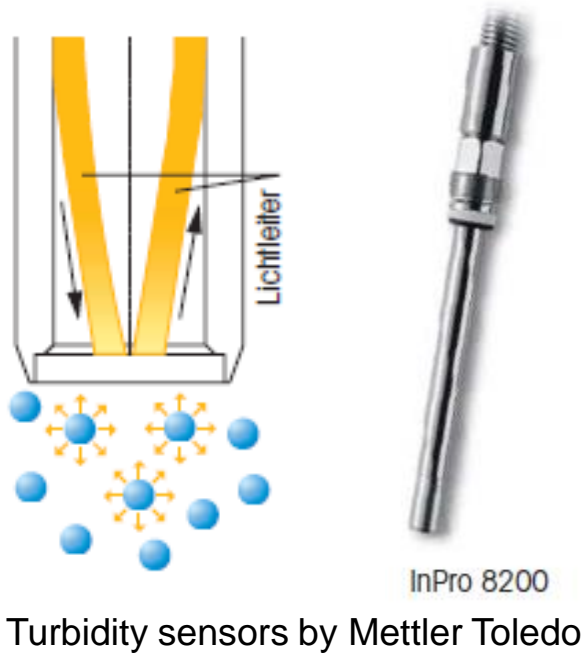
Nonlinearity due to swelling



Estimation of concentration and particle size challenging

Results from University of Hamburg

Turbidity → Particle Size Prediction (Semi-batch Process)

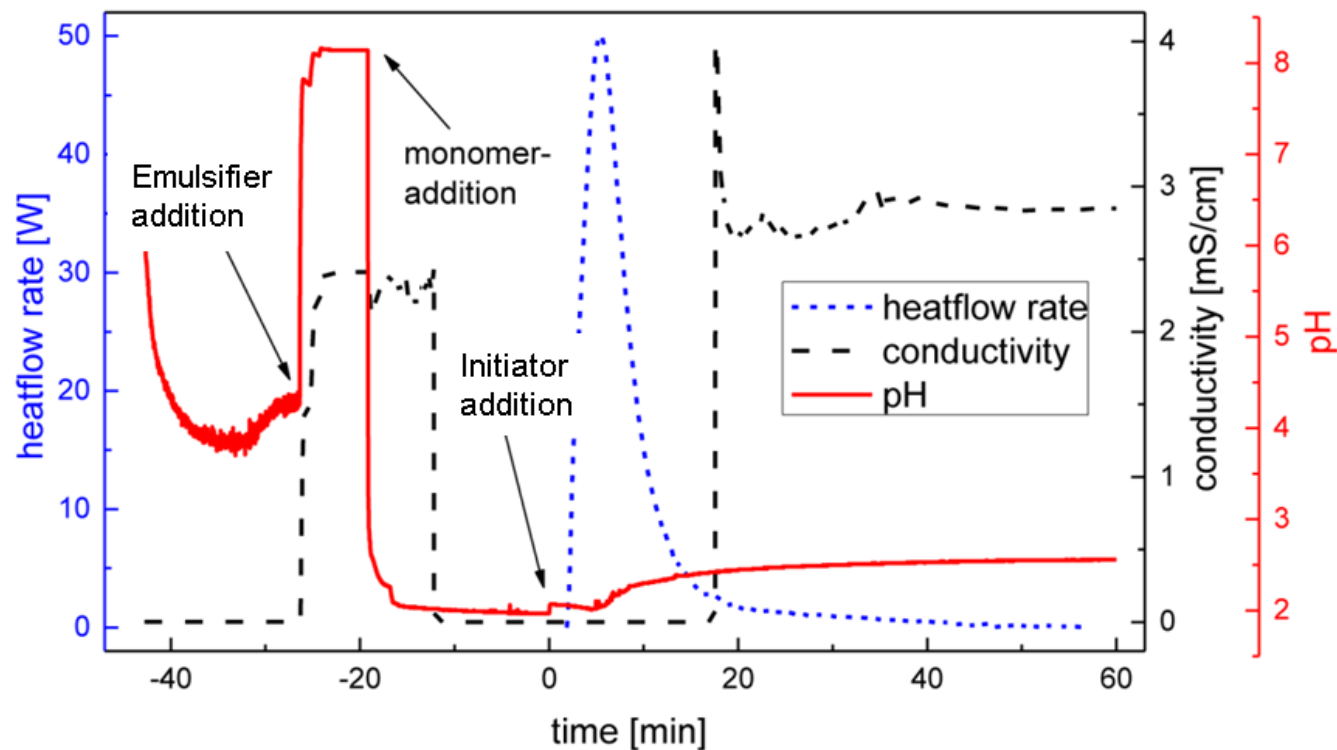


- Turbidity measurements in semi-batch reaction without effects of dosing.
- With sensor calibration turbidity leads directly to particle size.

Results from University of Hamburg

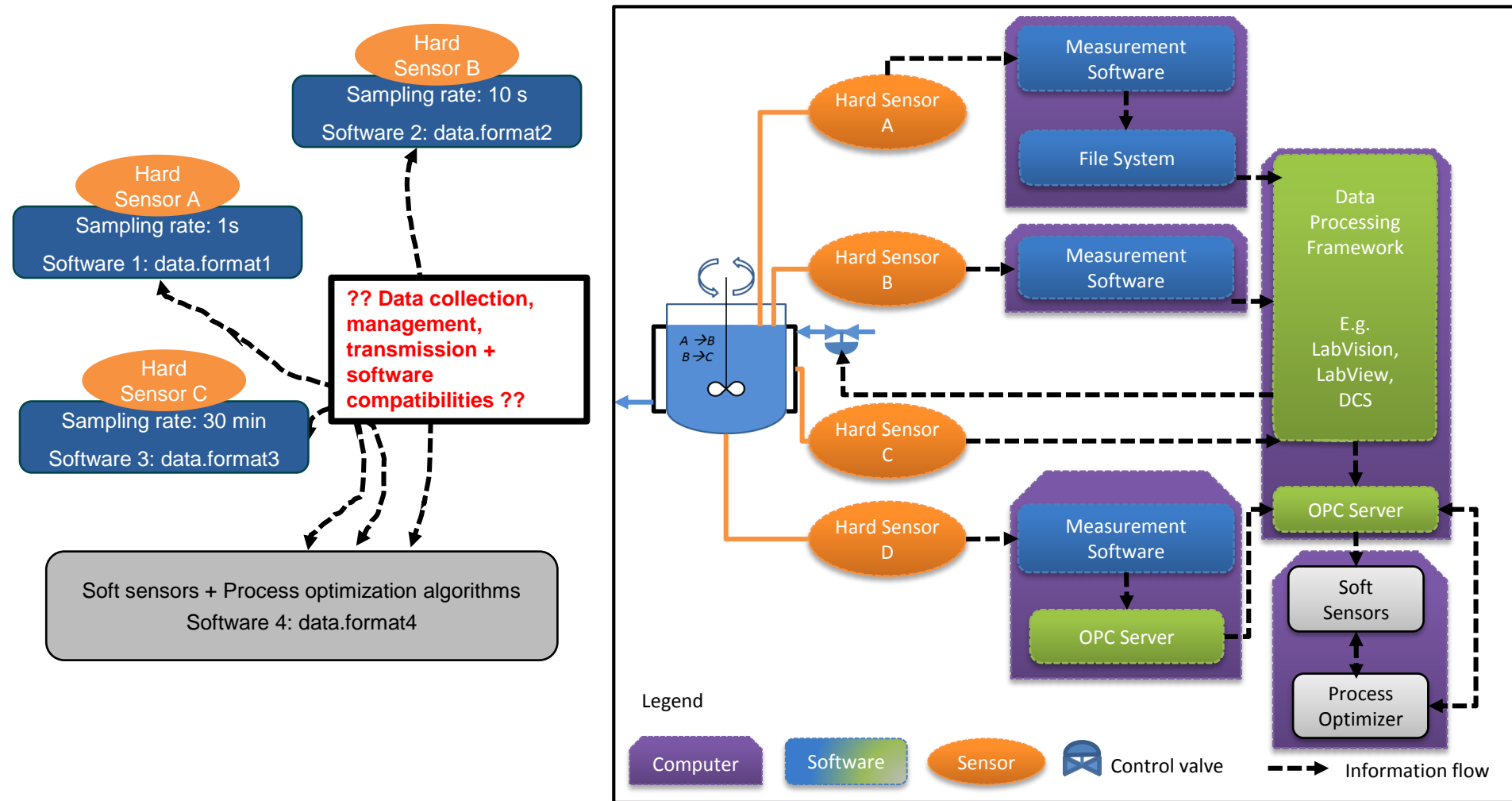
Other Sensors Investigated by Collaborators

- Conductivity measurements
- pH measurements



Results from University of Hamburg

OPC-based Data processing framework



- **Moments** of polymer chain length are **unobservable** without online measurements of polymer property.
- Linear observability analysis shows that **online concentration** measurements are required for **observability of energy and material balance** equations.
- **More parameters** are **identifiable** when **concentration measurements** are used along with calorimetric measurements.
- Problem of **suboptimal estimation** can be solved by using **deterministic global optimization** techniques.
- **Raman spectra** can be used to predict online **monomer conversions** and **particle size**.

Future Directions

- Modeling – developing models that **correlate measurements** (conductivity, pH, turbidity) to **process states** (particle sizes, polymer property).
- Sensor development – **sensor** for **online** monitoring of **polymer properties**.
- **Nonlinear** techniques for testing **observability** and **identifiability**.

Acknowledgments

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Thank you for your attention!

Questions?