

# Robust Optimizing Control of Chemical Processes

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# Outline

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- Motivation for robust optimizing control
- Industrial reactor example
  - A simple optimizing control scheme
- Model-based optimizing control
  - Online state and parameter estimation with simplified models
  - Online optimization
- Multi-stage optimizing control
  - Idea and problem formulation
  - Results for a case study
- Summary, limitations and further work

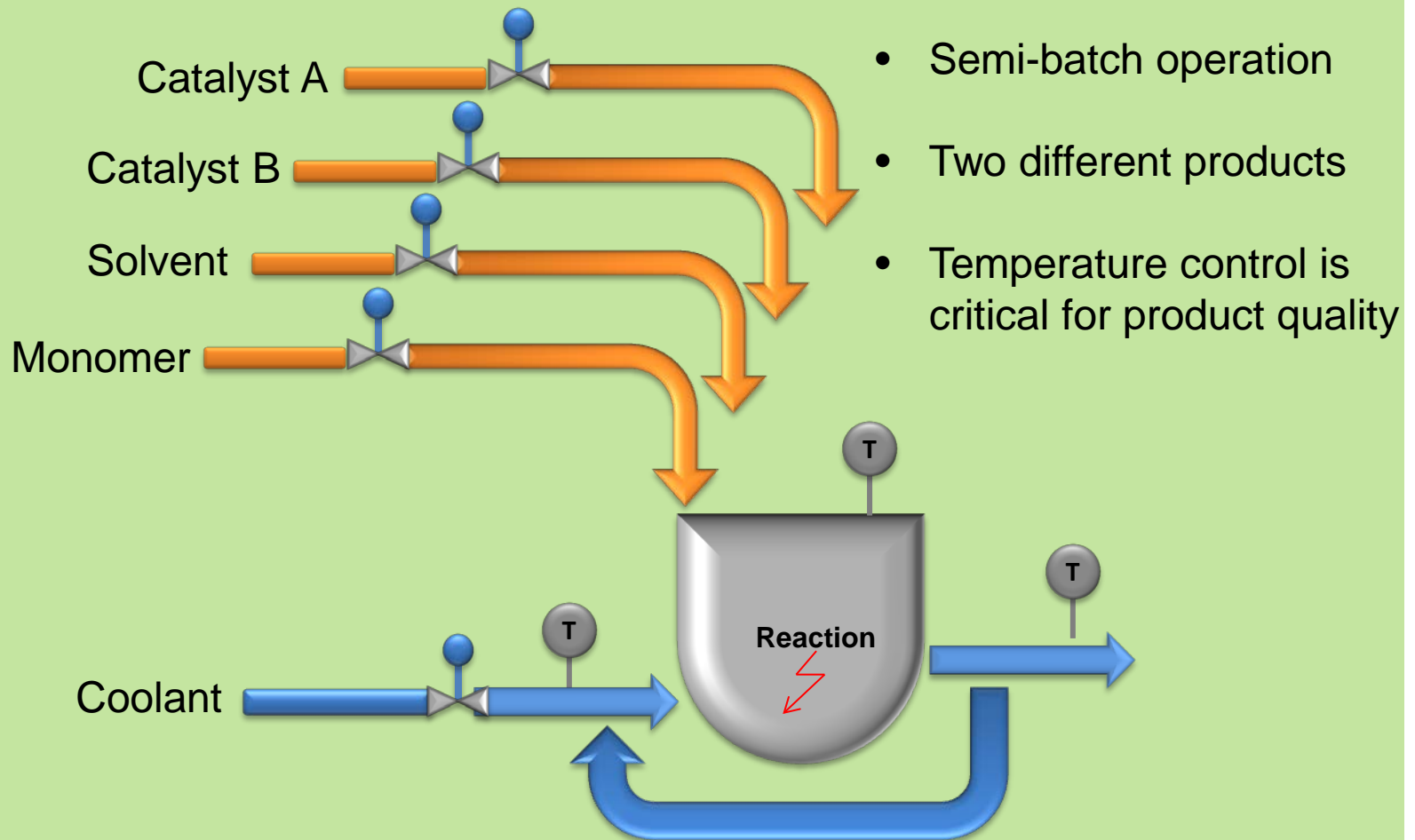
# Motivation for robust optimizing control

- **Operational excellence**
  - Optimal utilization of equipment and resources
  - Minimization of unplanned shut-downs
  - Meeting of quality standards without re-work
  - Energy efficiency
  - Resource efficiency
- Operations in the process industries are subject to significant uncertainties
  - Changing process behaviours (e.g. catalyst efficiency)
  - Changing equipment
  - Changing feeds
  - External influences as e.g. outside temperature
- **Efficient, safe and reliable operation requires reactive measurement-based optimization**

# Available technologies

- **Feedback control to track given set-points**
  - Requires a margin around the constraints
  - Set-points must be chosen well
- **Optimization of set-points and high-quality control (RTO plus MPC)**
- **Model-based optimizing control:**
  - The target of the controller is an economic optimization under constraints:
    - Safety limits
    - Product quality constraints
    - Equipment limitations
  - Depends critically on the accuracy of the model that is employed.

# Example: Industrial polymerization process

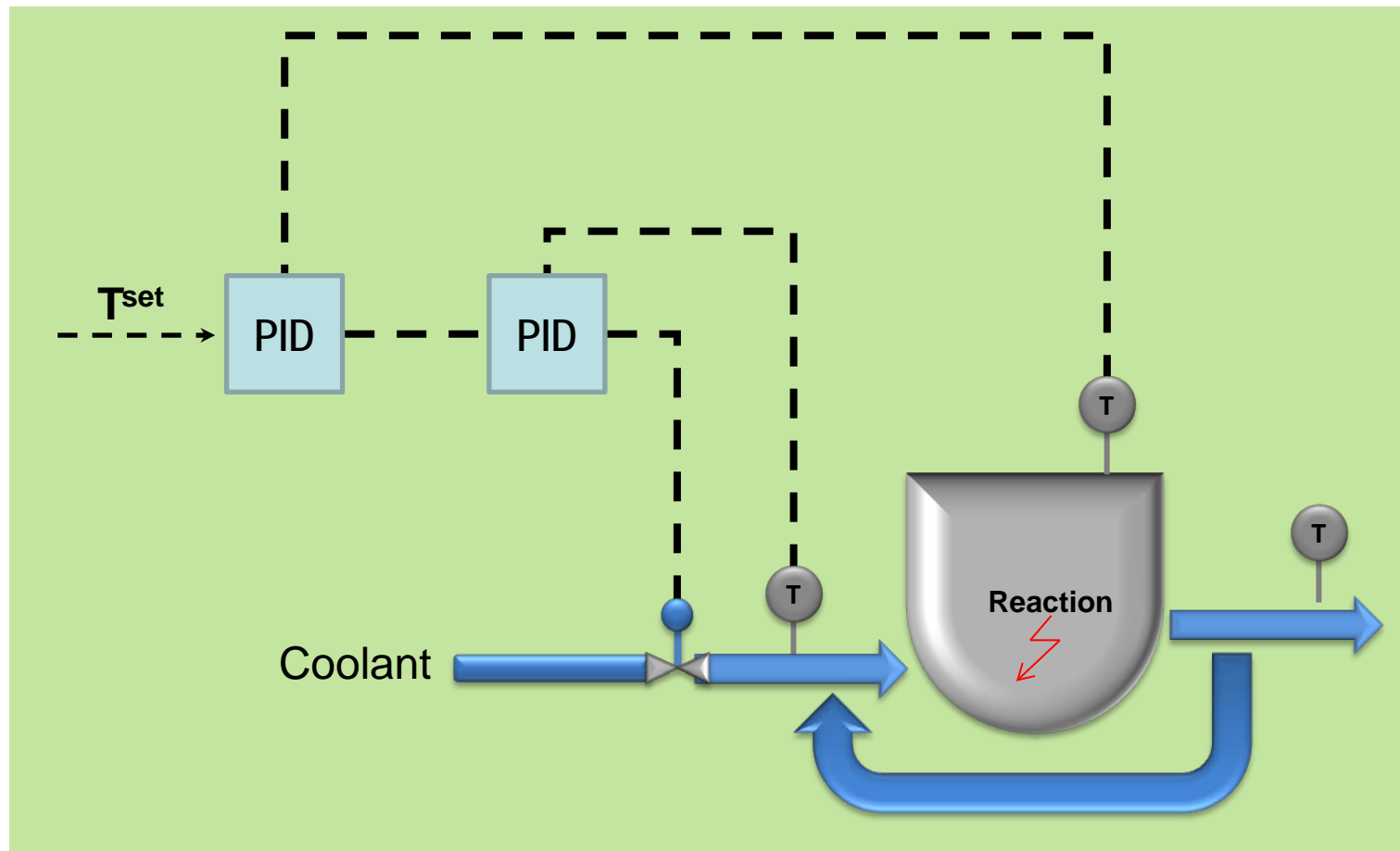




- **Goal:**
  - Demonstrate that advanced control can be used for the improvement of the operation of a real polymerization reactor
  
- **Project Partners:**
  - Evonik Industries
  - Leikon GmbH (Germany)
  - Process Dynamics and Operations Group (TU Dortmund)

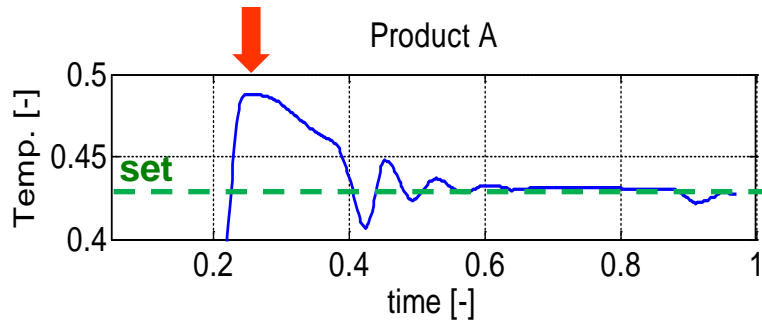
# Starting point

- Manual setting of the monomer feed rate
- Cascaded temperature control

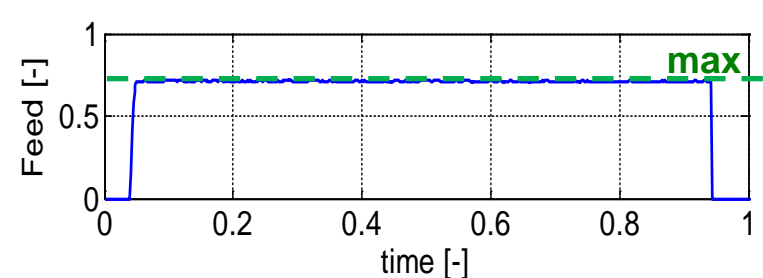
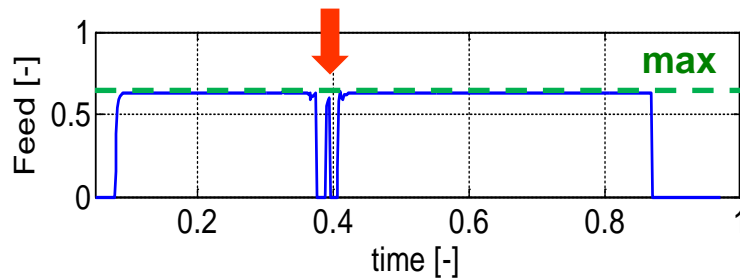
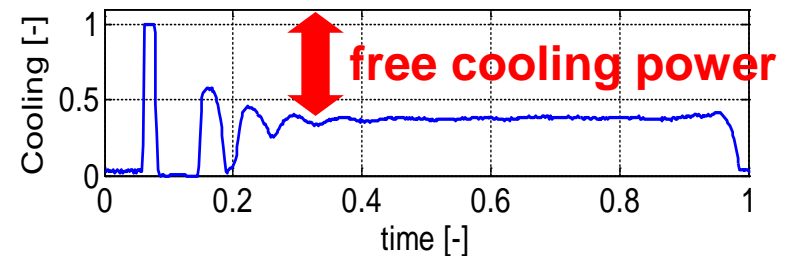
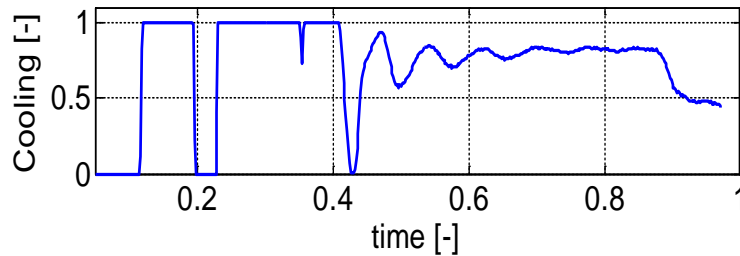
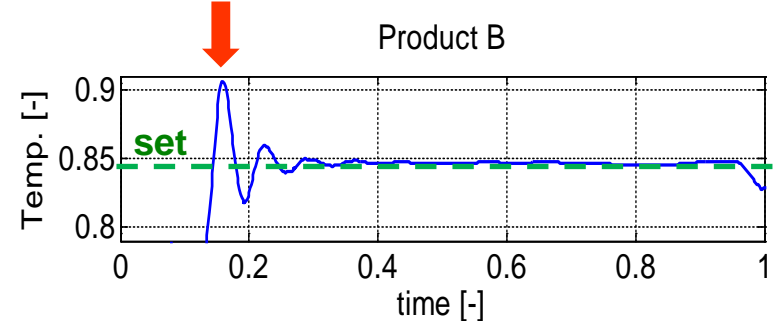


# Batch runs with the standard structure

temperature peak



temperature peak

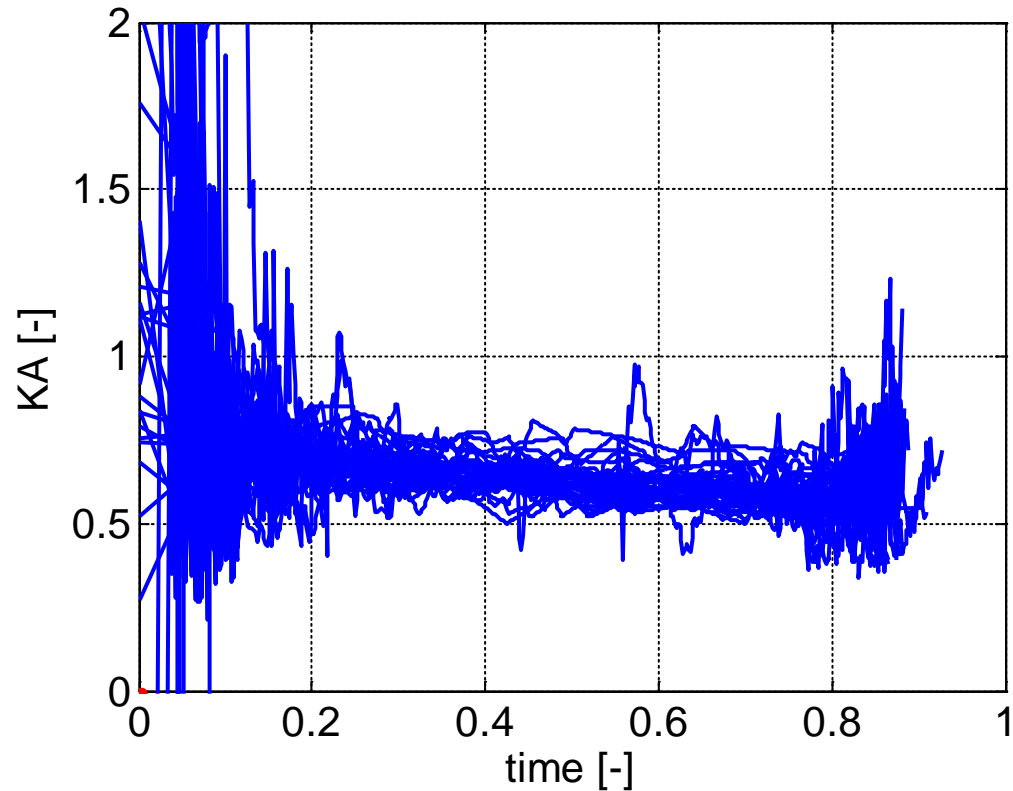




# Goal and first step

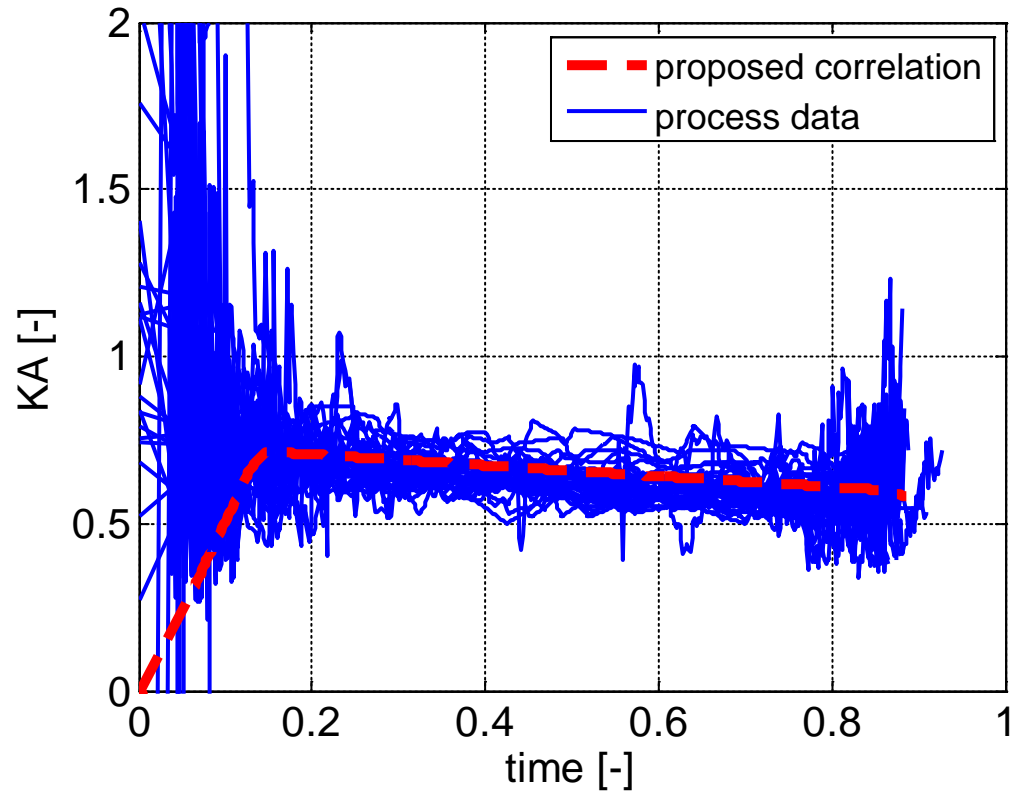
- Development of an advanced control solution that optimizes the setting of the coolant flow and the monomer feed rate for
  - Improvement of the temperature control
  - Increase of the productivity (shorter batch times)
- It all starts with modelling ...
- Standard polymerization reactor model
  - Energy and mass balances
  - Reaction mechanism available in the literature
  - Equations for reaction rates, heat transfer coefficient, cooling power
  - Model for polymer chain growth

# Empirical correlation for KA



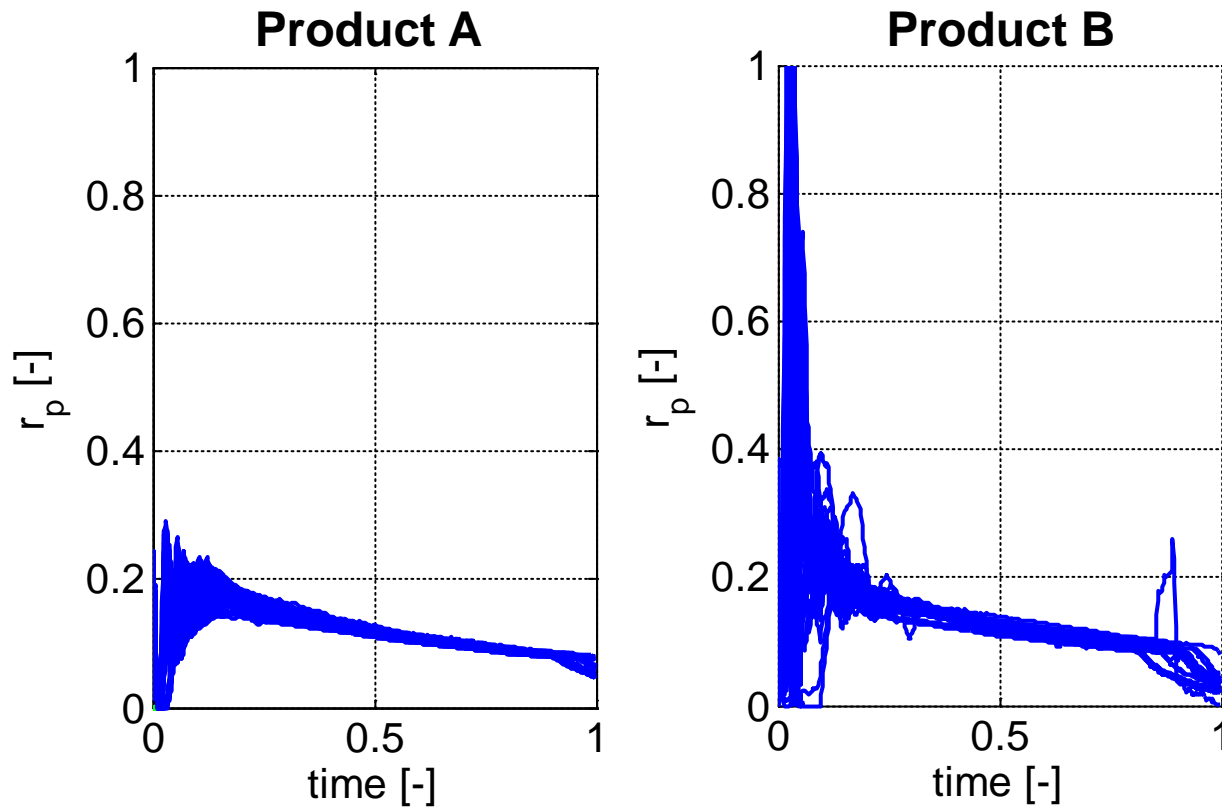
$$KA = \frac{CP_J M_J \frac{dT_J}{dt} - F_{cool} CP_W (T_{cool} - T_{J_{out}})}{(T_R - T_J)}$$

# Empirical correlation for KA



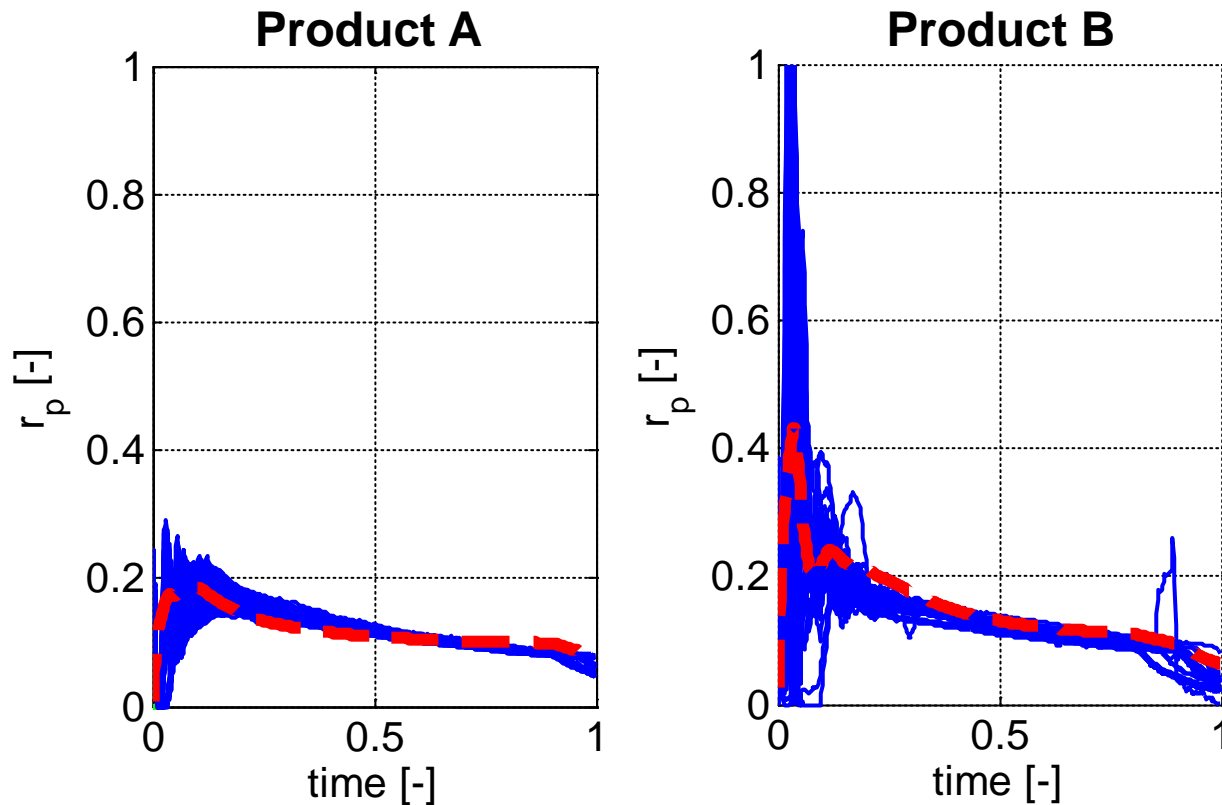
$$KA = C_1 M_R(t) - C_2 M_P(t)$$

# Estimation of the reaction constants



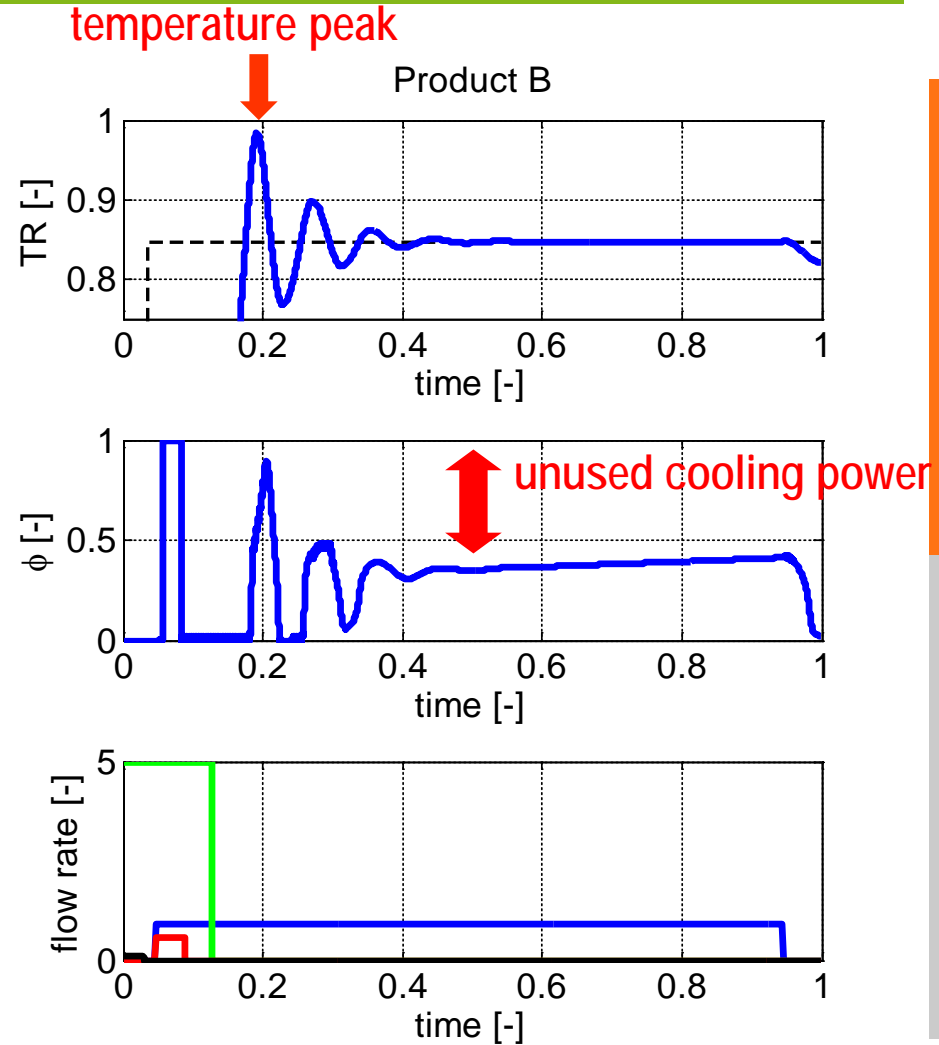
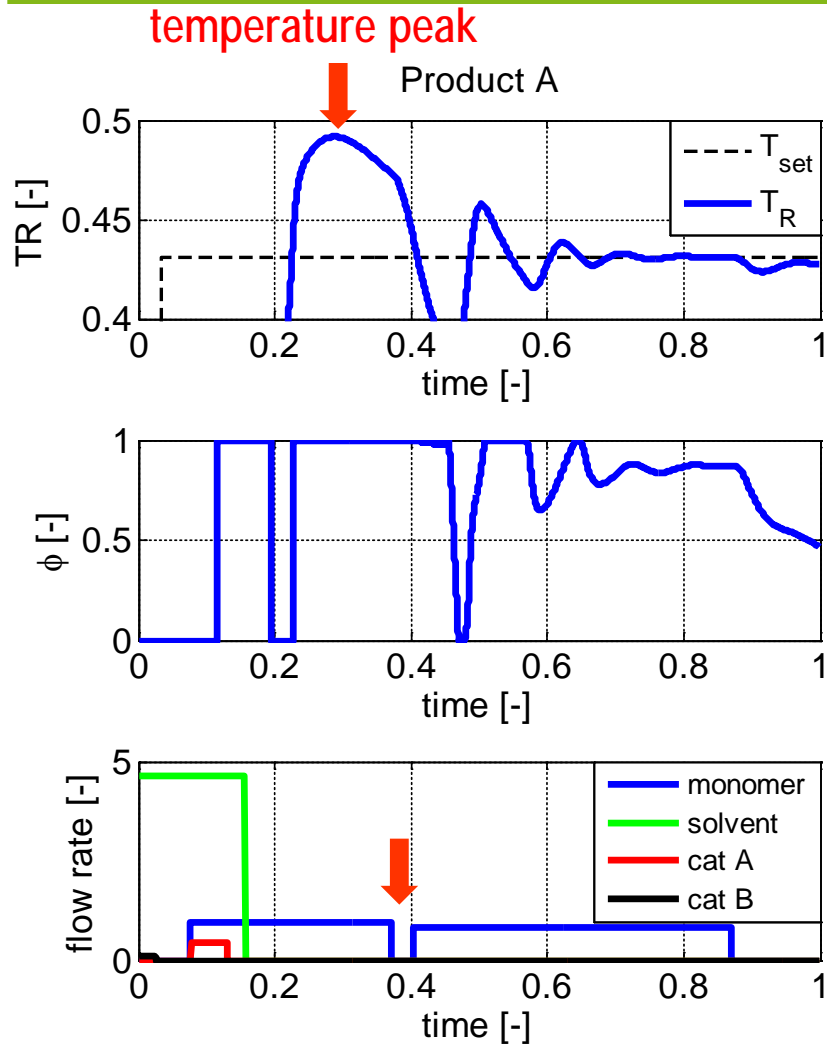
$$r_P = \frac{C_{P_R} M_R \frac{dT_R}{dt} - KA(T_J - T_R) - \sum_{i=S,M} F_i C_{P_i} (T_i - T_R)}{\Delta H_R}$$

# Estimation of the reaction rate constants



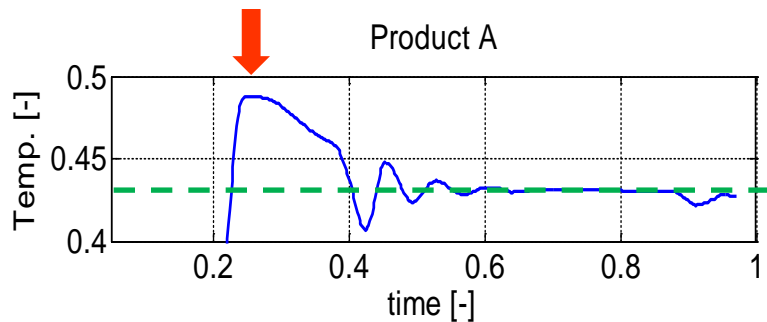
$$r_p = k_1 \exp\left(\frac{-Ea_1}{RT_R}\right) C_{P_{1,r}^*} C_M + k_2 \exp\left(\frac{-Ea_2}{RT_R}\right) C_{P_{2,r}^*} C_M$$

# Closed-loop simulations

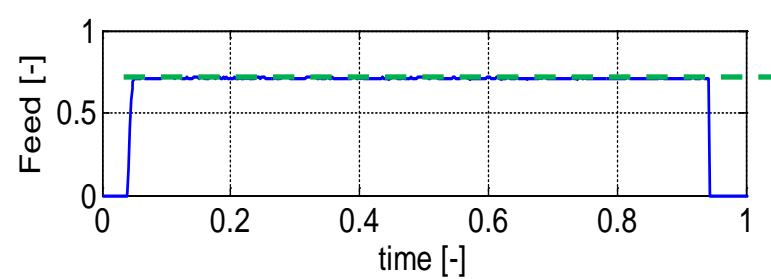
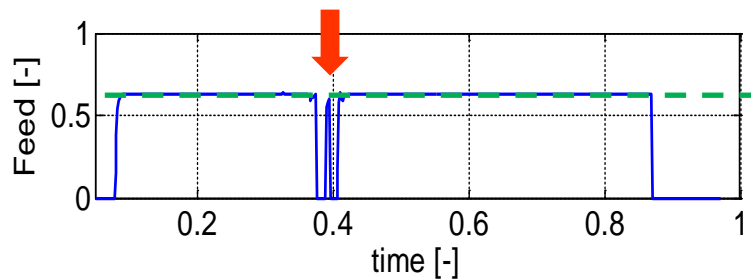
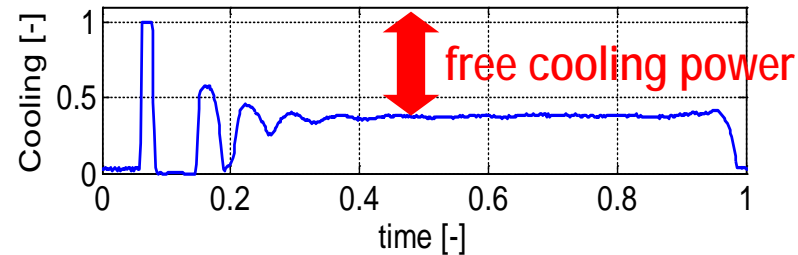
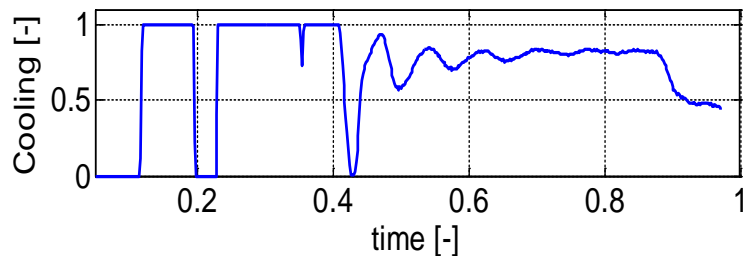
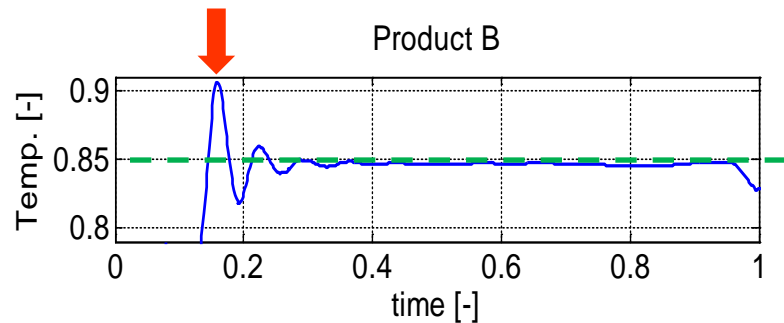


# Real batch runs

temperature peak



temperature peak



# Next step: Control solution

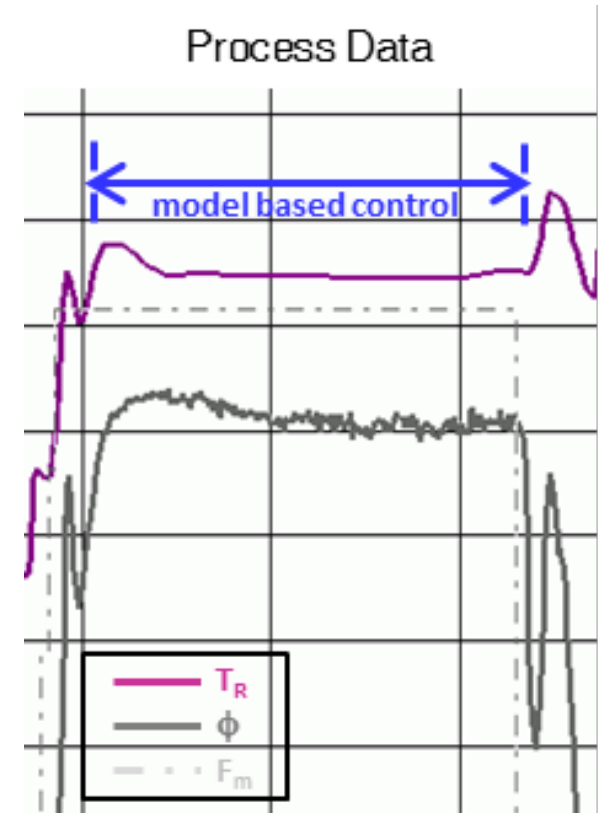
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- So now we have a model – but of course the model is not exact
- Should we build a model-based controller upon it?
- How to take uncertainties into account?
  
- **Solution 1:**
  - MPC controller of the temperature (model-based, identified model)
  - Simple optimizing monomer flow controller
  
- **Solution 2:**
  - Model-based optimizing control using state and parameter estimation



# Improved temperature control

- A version of MPC of the temperature was integrated into the DCS of the real process
- The temperature peak was reduced to less than 0.5 K.
- The controller is used to control the temperature of the industrial reactor.

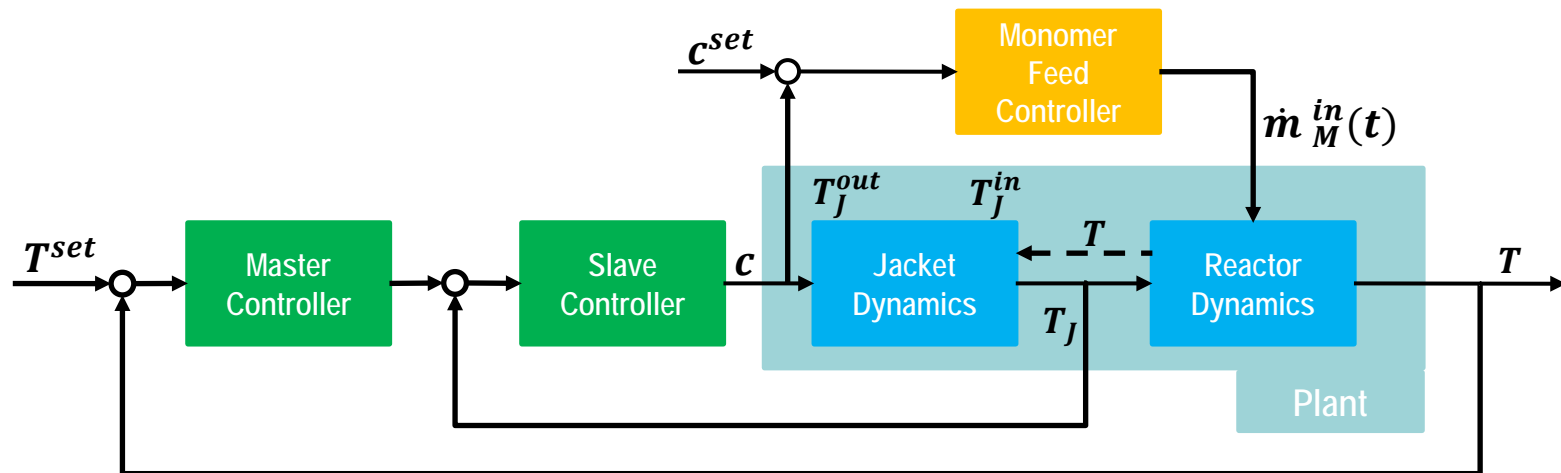


# Near optimal operation by simple feedback control

- Idea:

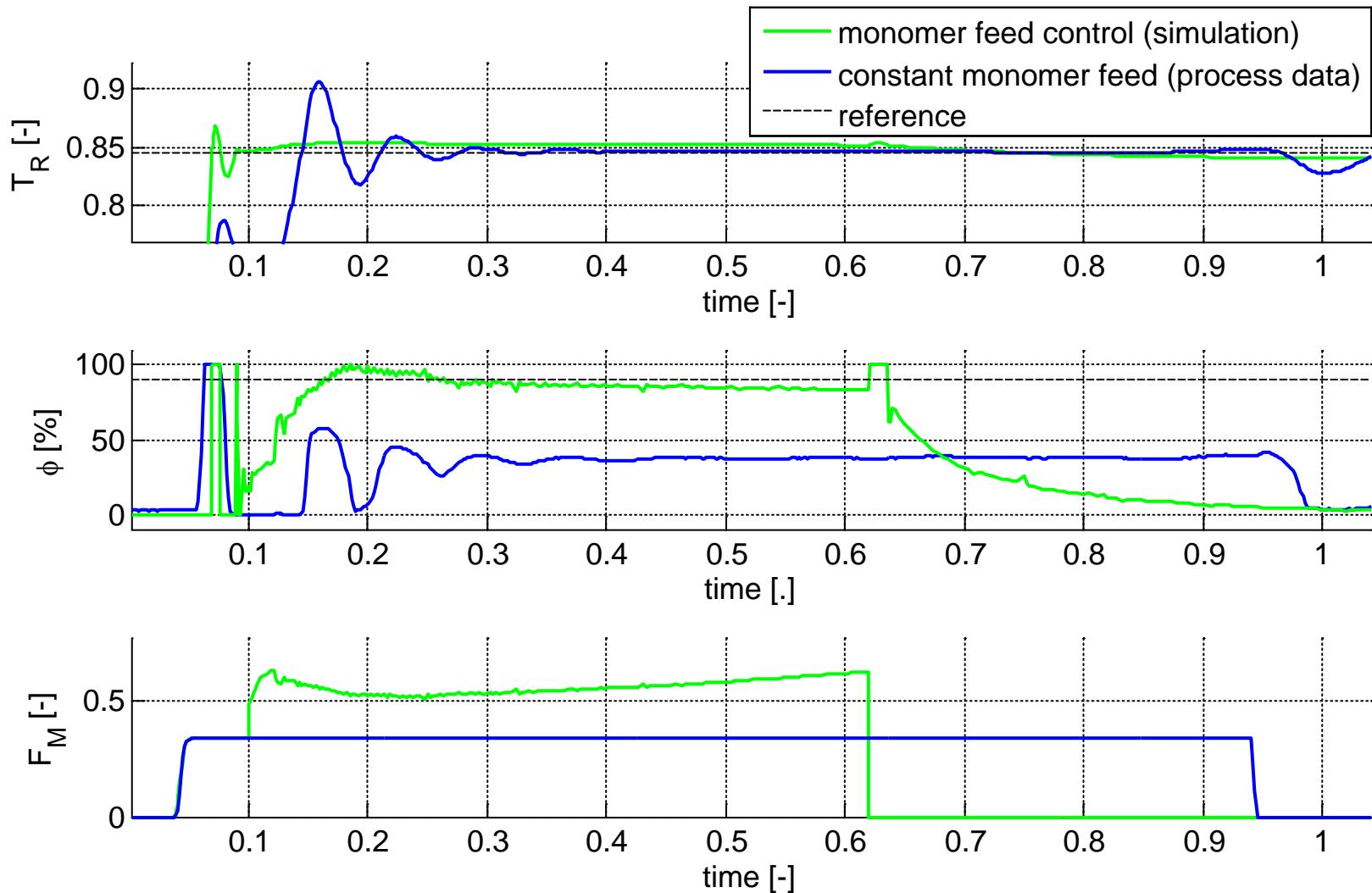
Instead of online optimization, use a feedback controller that establishes an optimal operation (NCO tracking)

- Here: Make **full use of the available cooling power**



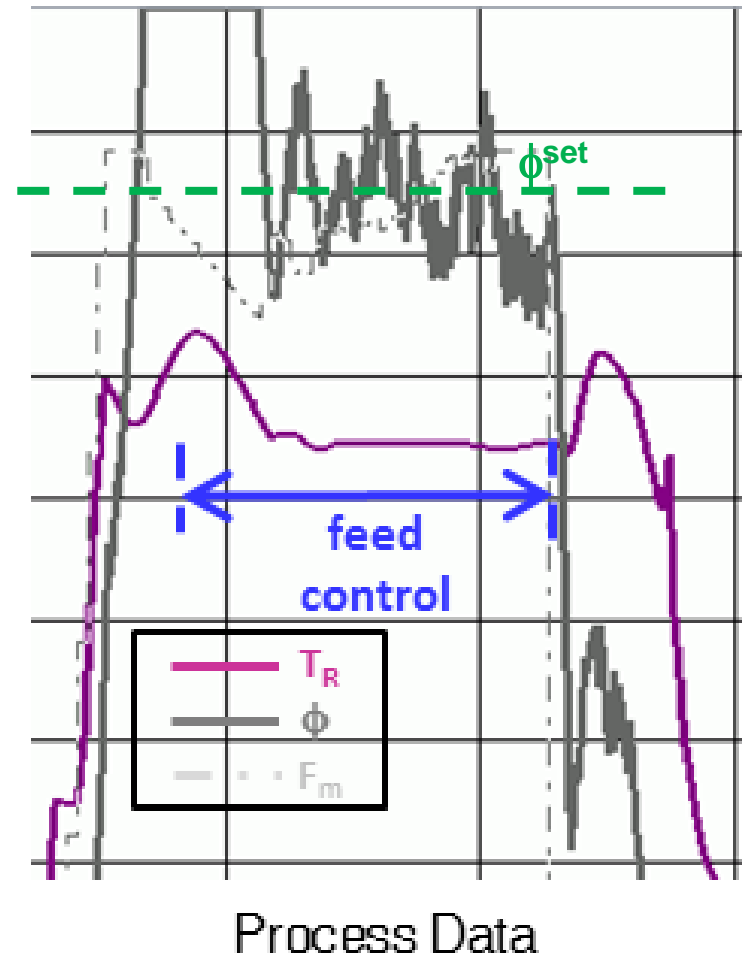
- Parameter  $c^{set}$  determines the spare cooling power

# Monomer feed control simulated for the industrial case

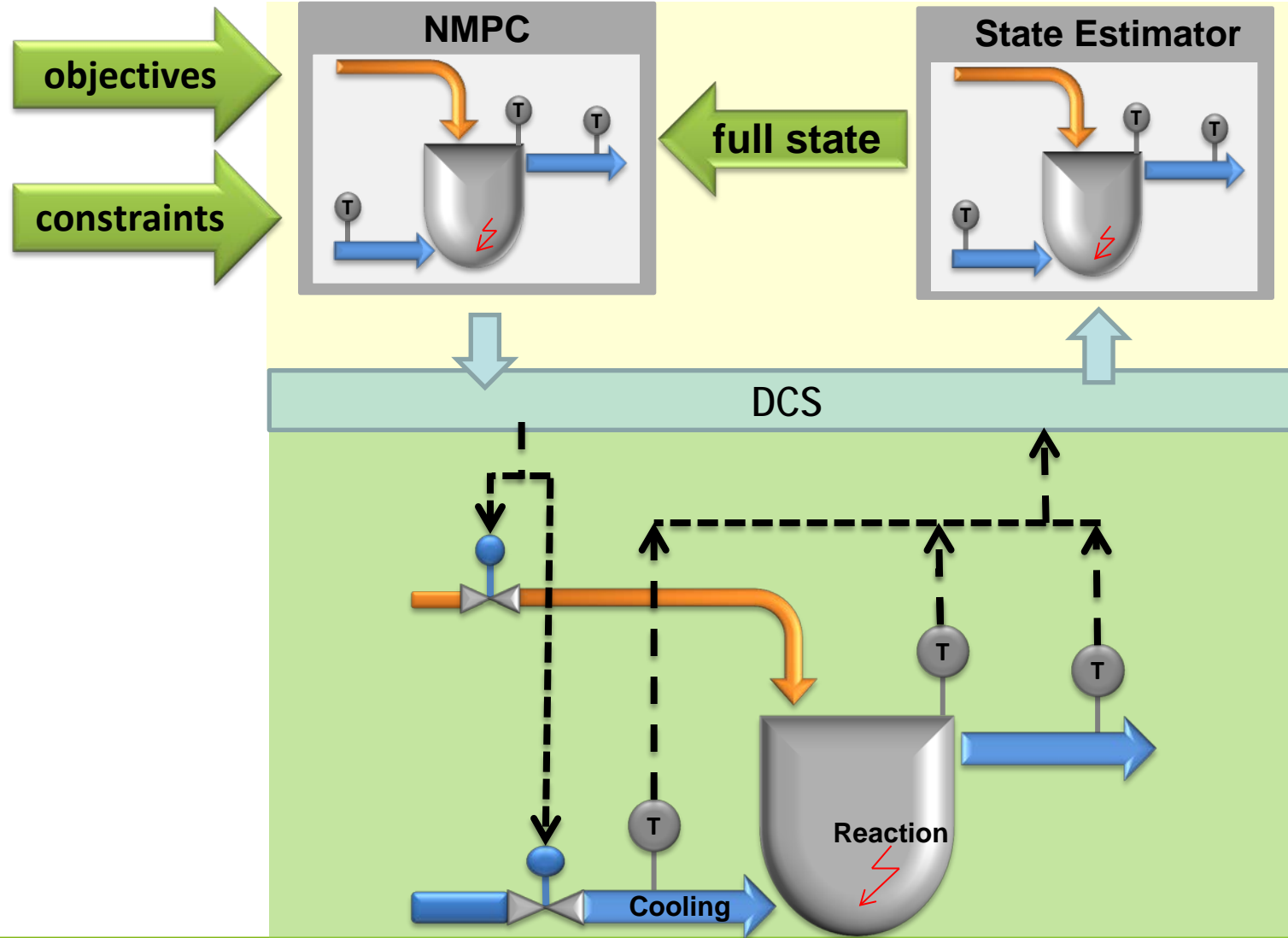


# Implementation results

- Feedback controller for the monomer feed implemented at the plant
- Easy to realize in the DCS
- Successful stable operation
- Better temperature control thanks to the MPC controller and 25% reduction of the feeding times achieved
- Accepted by the operating crew
- **In daily operation!!**

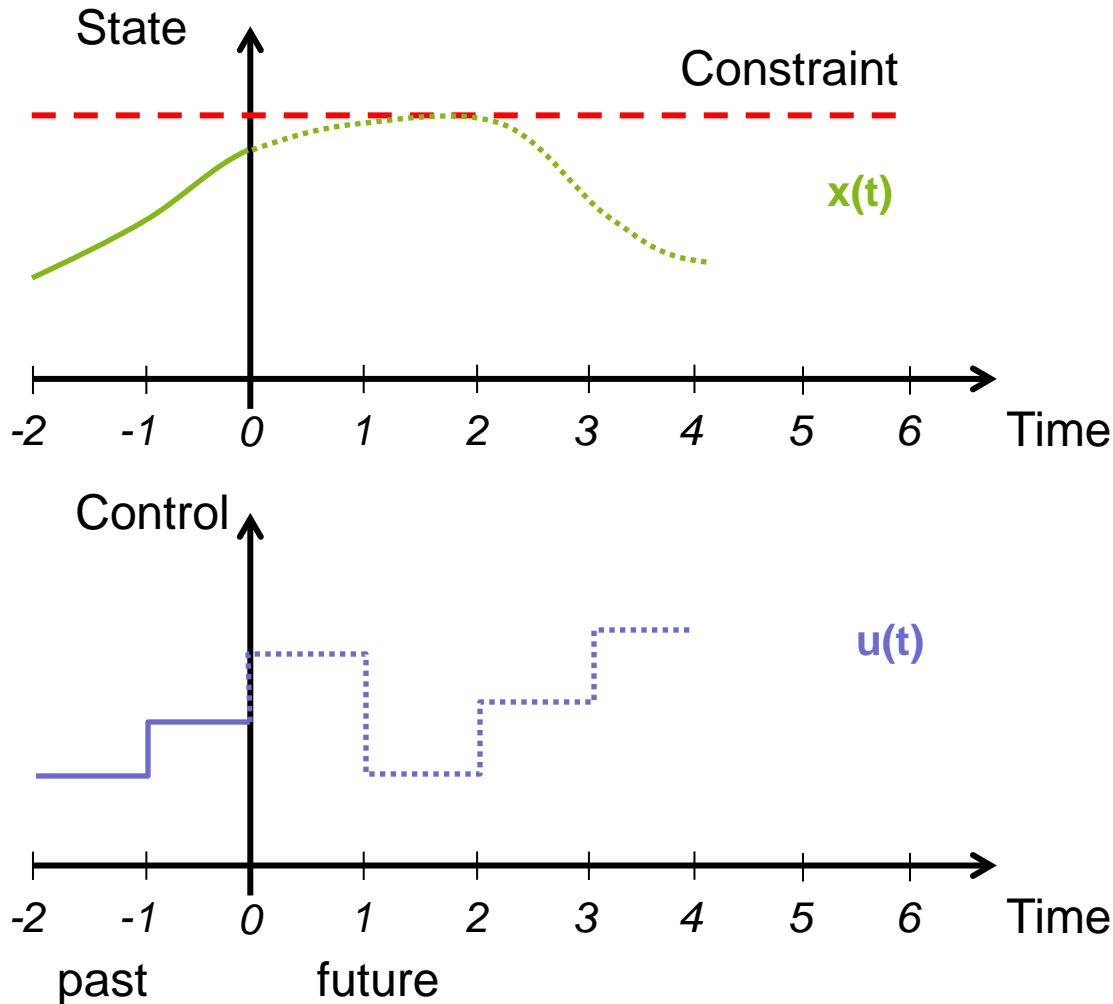


# Model-based control scheme



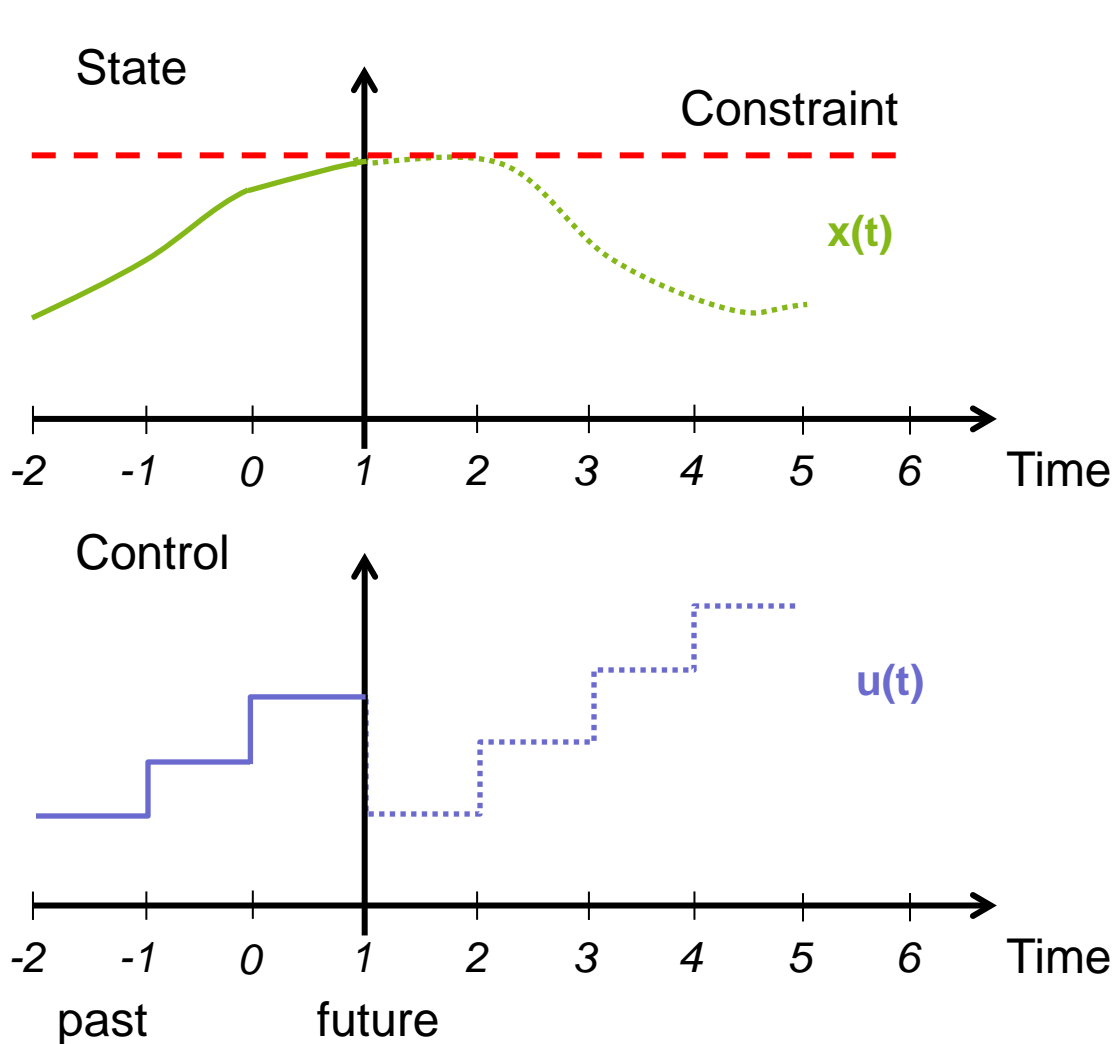
# Model predictive control

## MPC



- Solve optimization problem
  - Mathematical Model
  - Cost function
  - Constraints
- Apply first control input

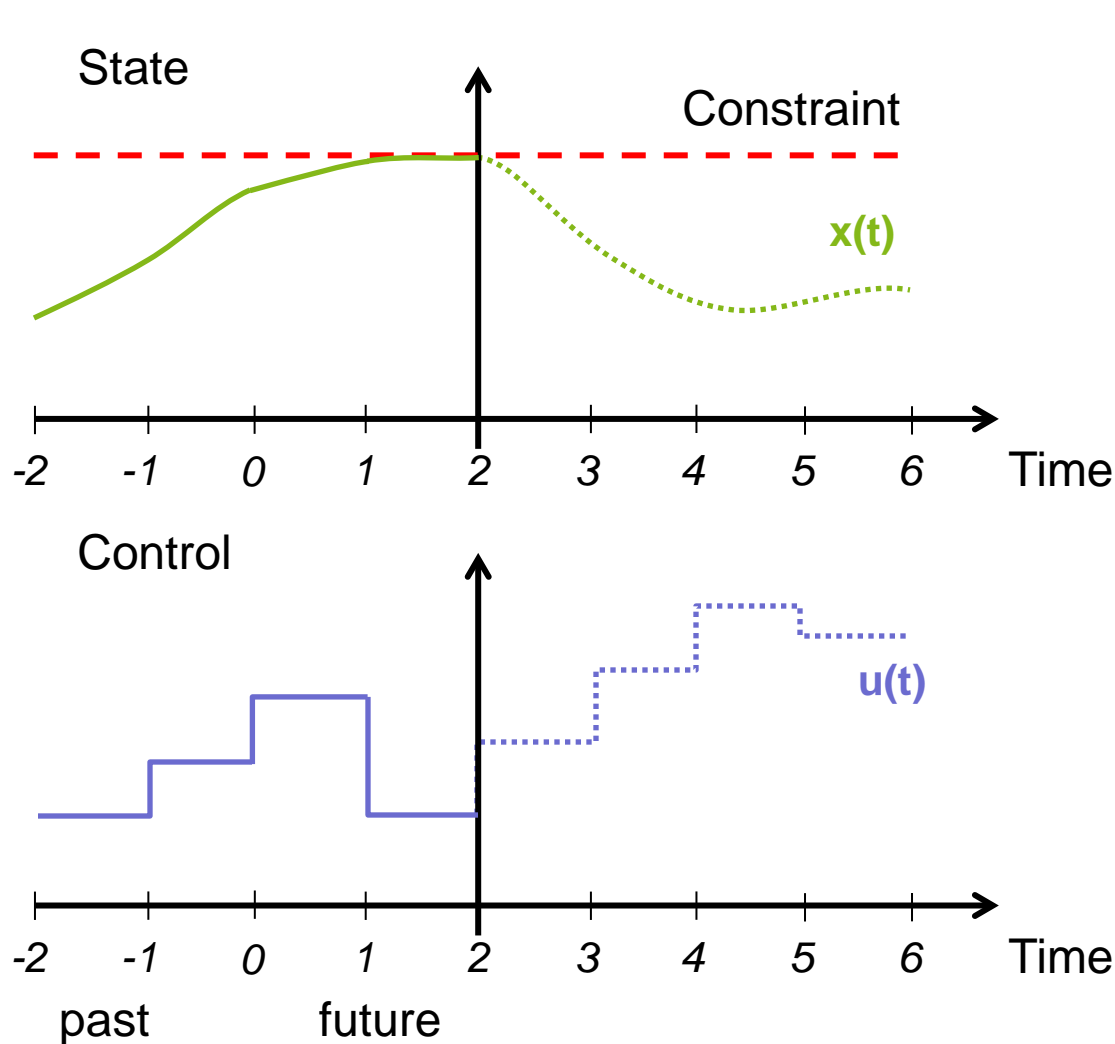
# Model predictive control



## MPC

- Solve optimization problem
  - Mathematical Model
  - Cost function
  - Constraints
- Apply first control input
- Take new measurements
- Optimize again

# Model predictive control

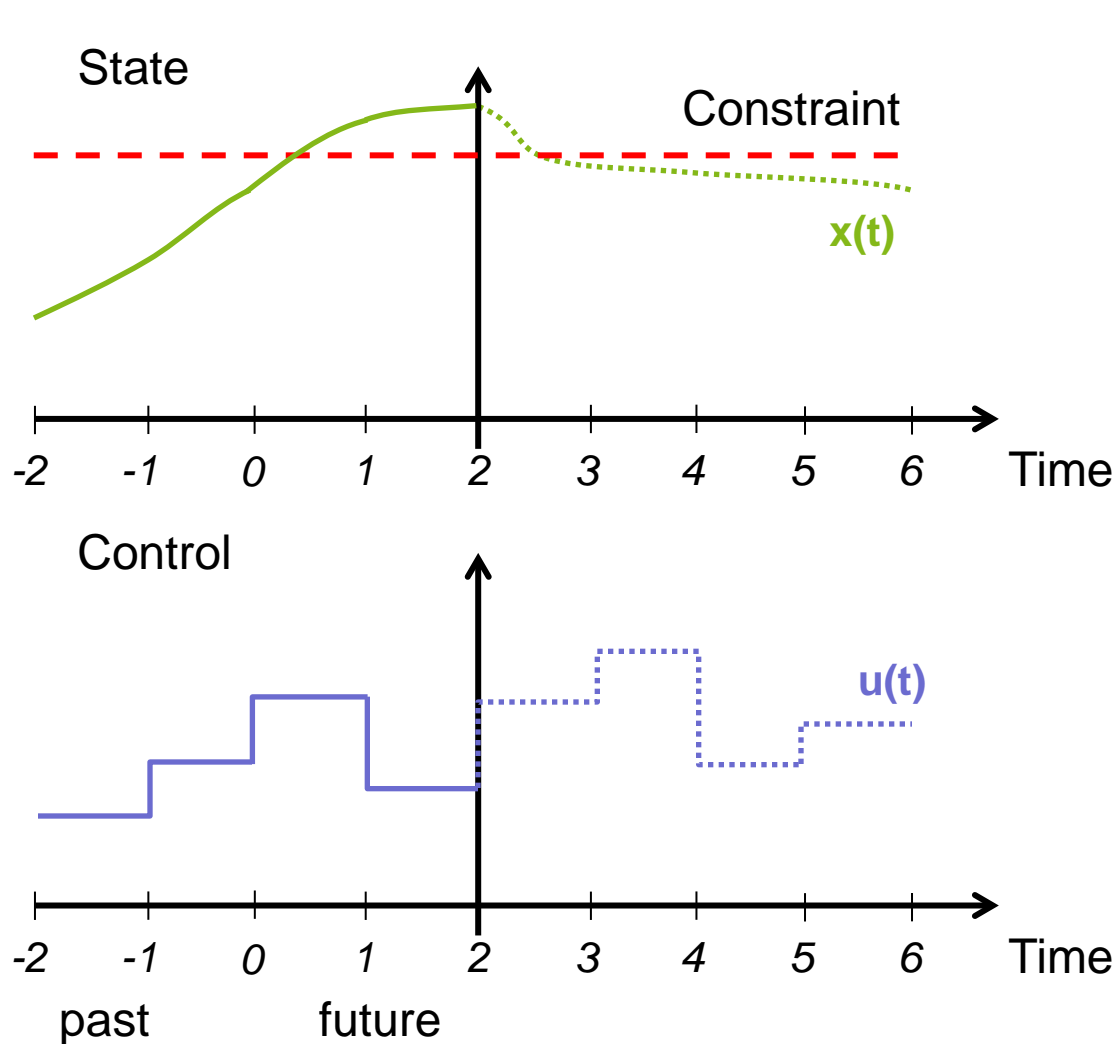


## MPC

- Solve optimization problem
  - Mathematical Model
  - Cost function
  - Constraints
- Apply first control input
- Take new measurements
- Optimize again
- Apply first control input
- Take new measurements and optimize again ....
- Economic cost function can be used in the optimization  
→ optimizing control



# Model Predictive Control: Wrong model



## MPC

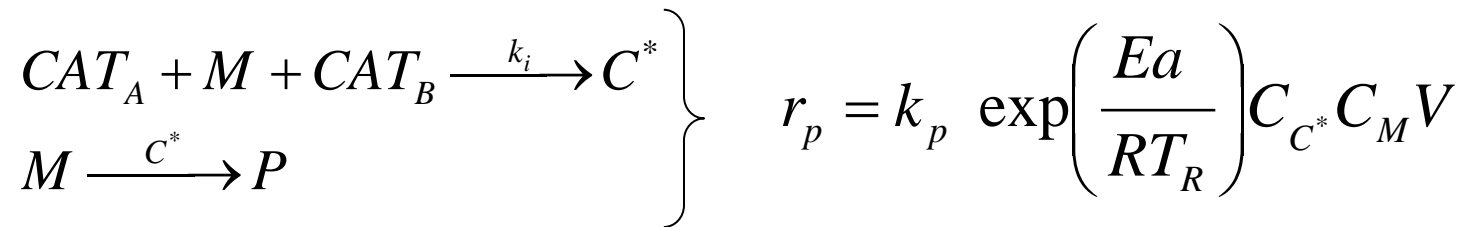
- Solve optimization problem
  - Mathematical Model
  - Cost function
  - Constraints
- Apply first control input
- Take new measurements

What happens if the prediction is not exact?

- Violation of constraints
- Decreased performance
- Instability

# Industrial example – online model adaptation

- Reduced model
  - 6 mass balances, 3 energy balances, 6 moment balances
- Simplified kinetics:

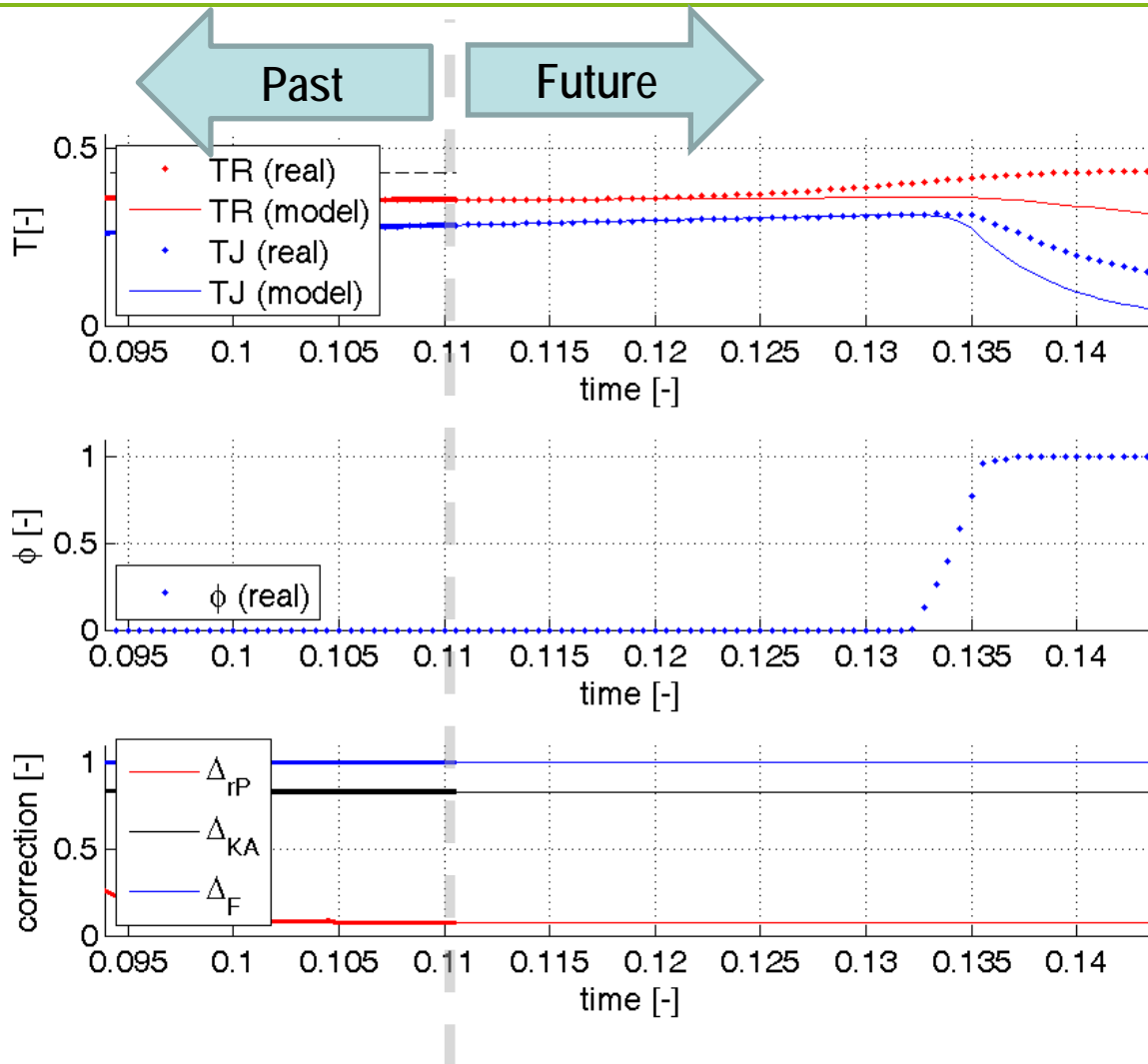


- Online compensation of uncertainties:

$$\left\{ \begin{array}{l} r_p^* = \left( k_p \exp\left(\frac{Ea}{RT_R}\right) C_{C^*} C_M V \right) \Delta_{r_p} \\ KA^* = (C_1 M_R(t) - C_2 M_P(t)) \Delta_{KA} \\ F_{cool}^* = (\beta_1 \phi + \beta_2 \phi^2 + \beta_3 \phi^3 + \beta_4 \phi^4) \Delta_{F_{cool}} \end{array} \right.$$

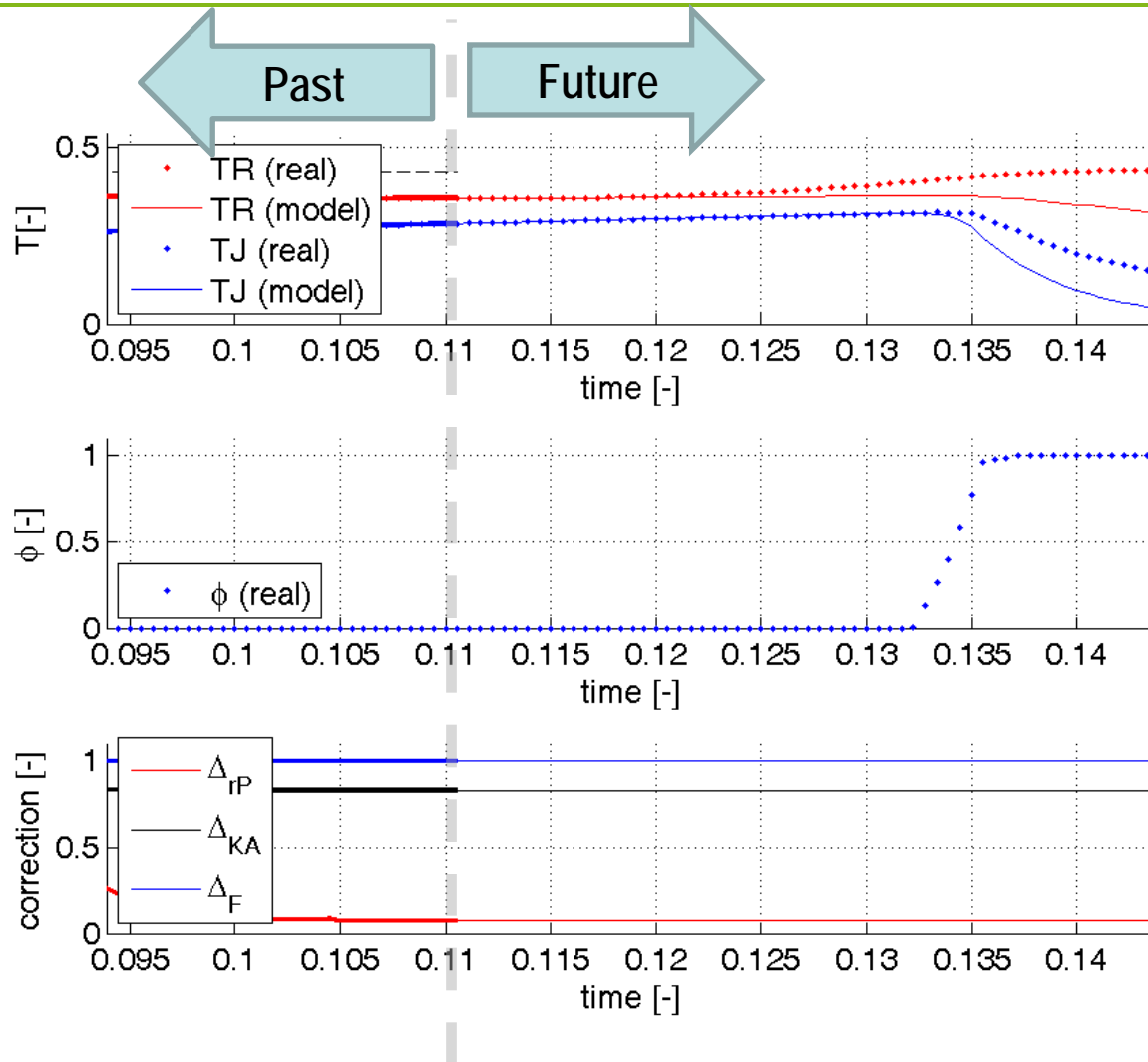
Correction factors are  
estimated by the state  
estimator.

# Testing for real batch data



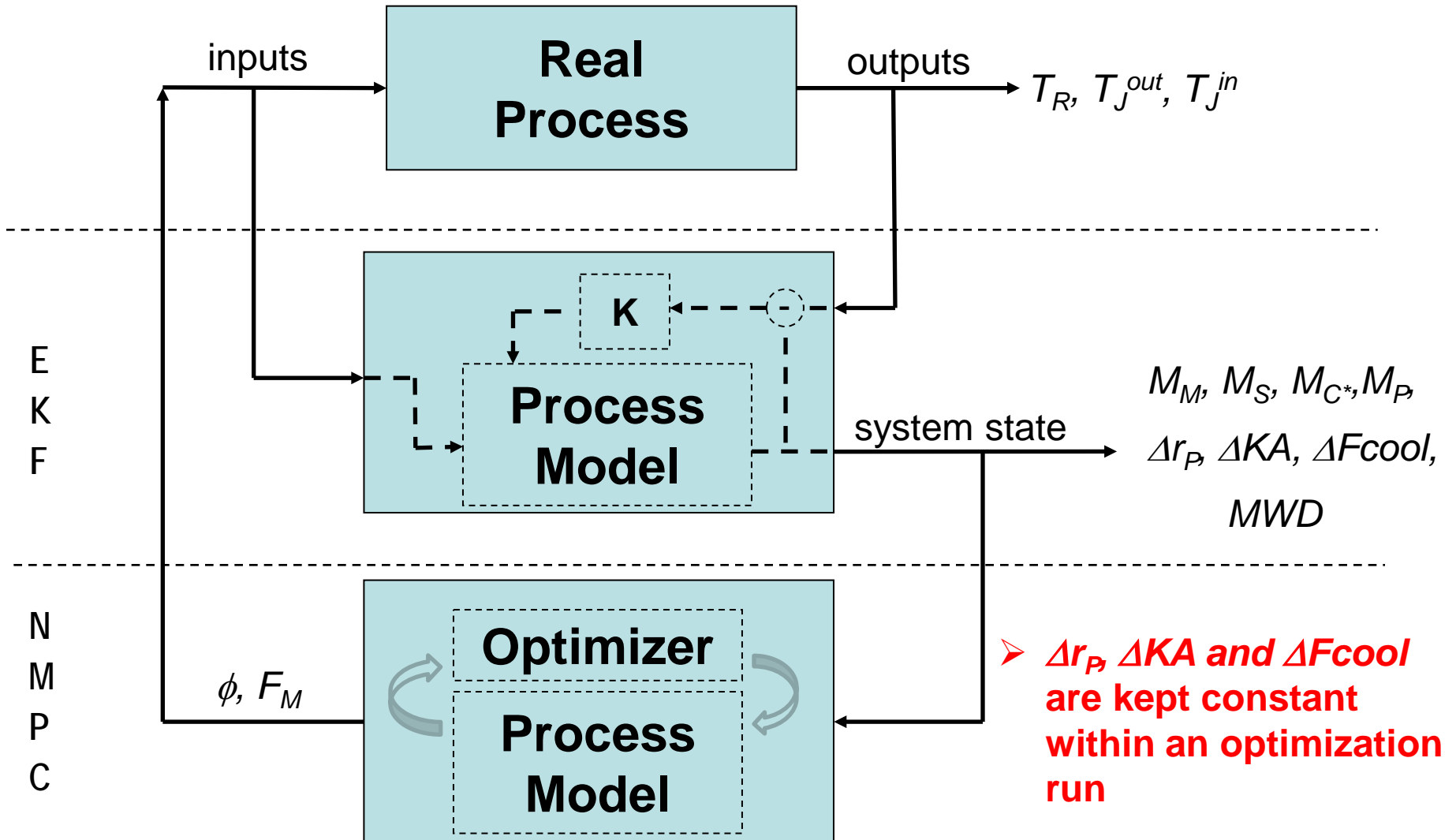
- Measurements taken from a real batch (dots)
- The measurements are fed to the EKF and the correctors are updated.
- The model is repeatedly simulated from the current time point (continuous lines)
- The correctors are kept constant during each simulation.

# Testing for real batch data



- Measurements taken from a real batch (dots)
- The measurements are fed to the EKF and the correctors are updated.
- The model is repeatedly simulated from the current time point (continuous lines).
- The correctors are kept constant during each simulation.

# Block diagram of the closed-loop

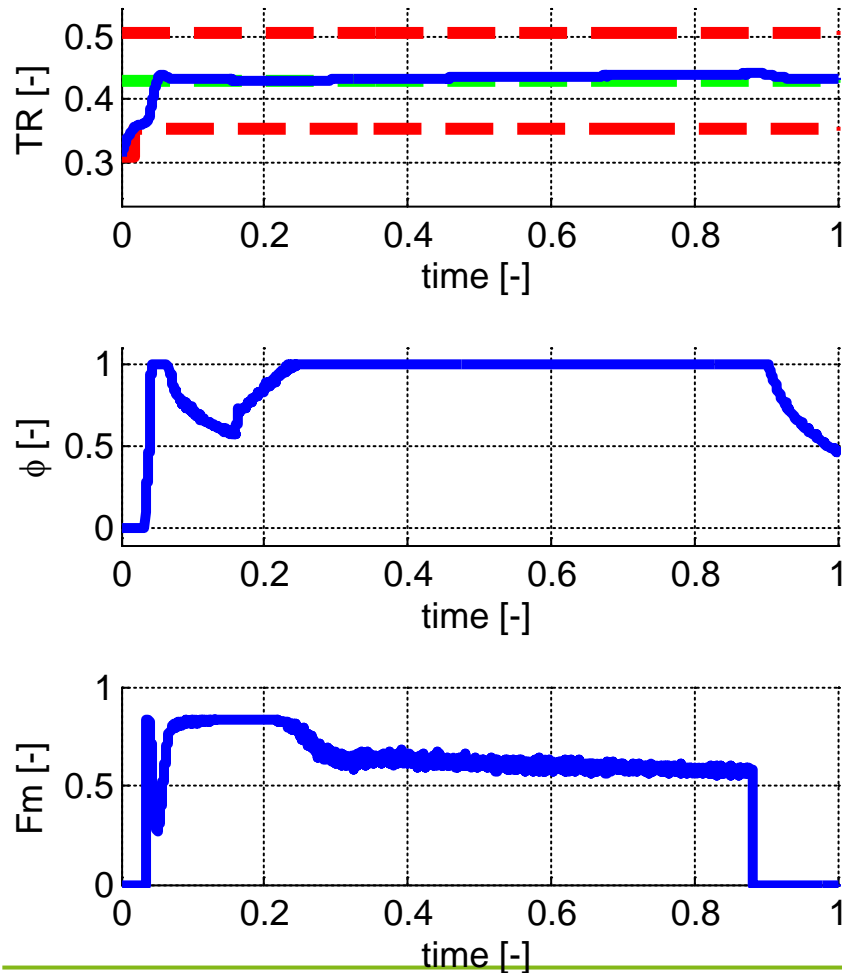


# NMPC simulation

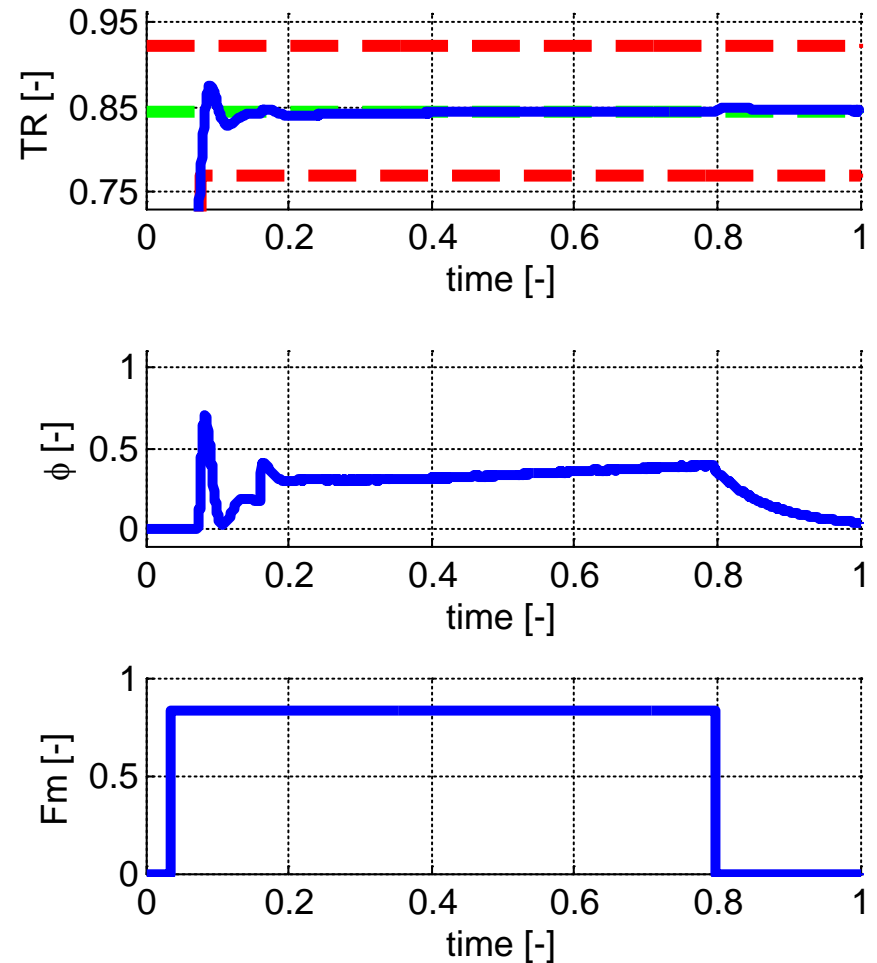
- NMPC setup was intensively tested by simulations
- Controller Settings:
  - Prediction horizon: 10 minutes
  - Control horizon: 10 minutes
  - Discretization period: 2 minutes
  - Sampling period: 10 seconds
- Plant-model mismatches:
  - reaction rate:  $\pm 50\%$
  - heat transfer efficiency:  $\pm 25\%$
  - cooling capacity:  $\pm 50\%$

# Simulation (Normal reactivity)

## Automatic Monomer Feed (Product A)

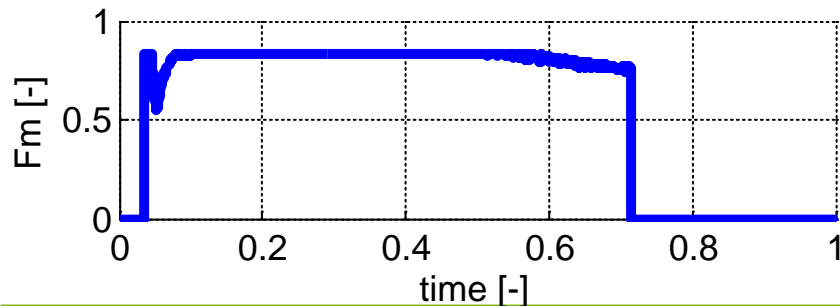
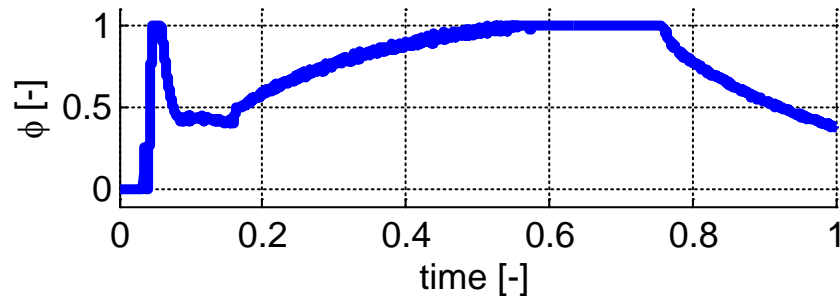
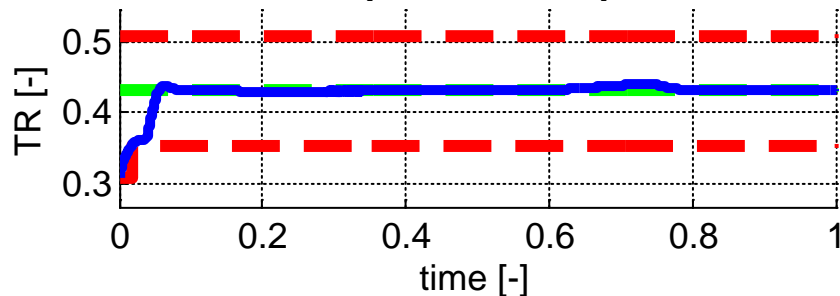


## Constant Monomer Feed (Product B)

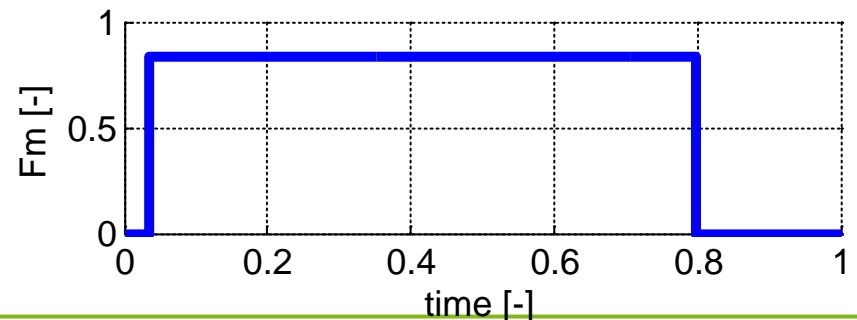
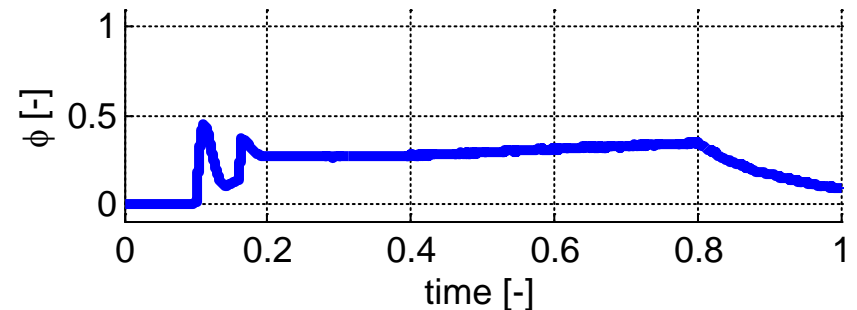
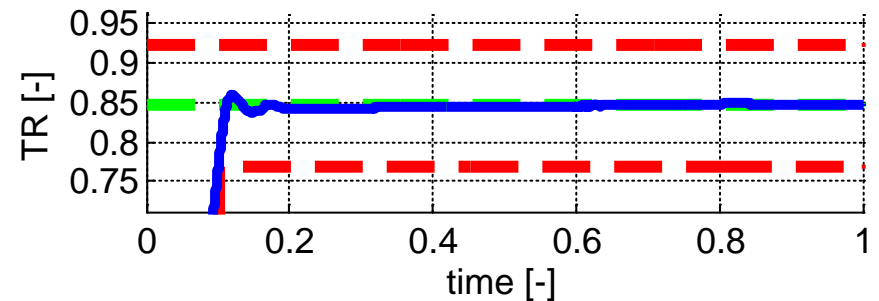


# Simulation (Low reactivity)

## Automatic Monomer Feed (Product A)



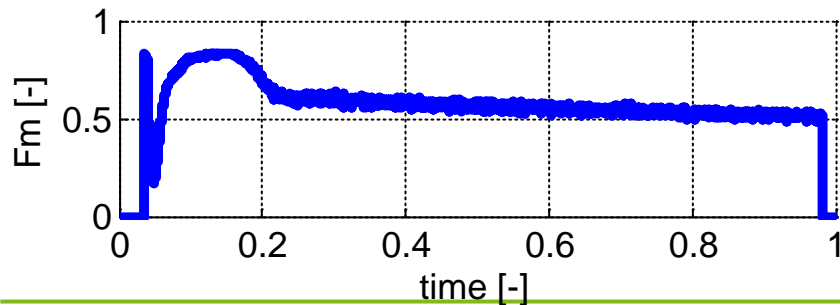
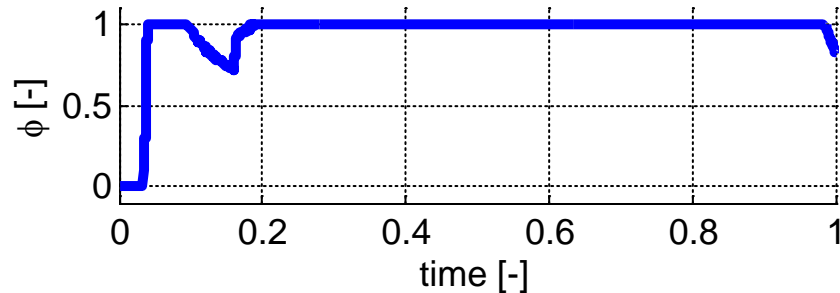
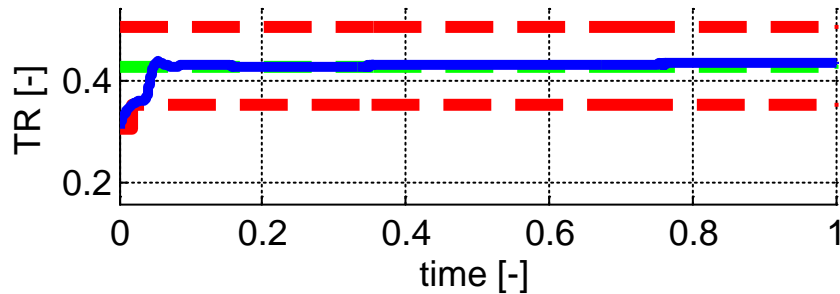
## Constant Monomer Feed (Product B)



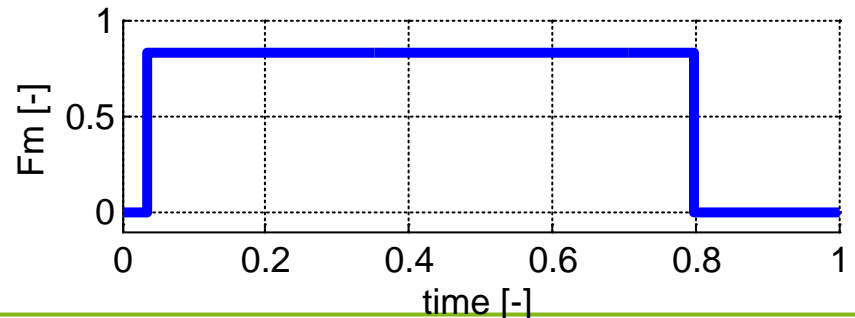
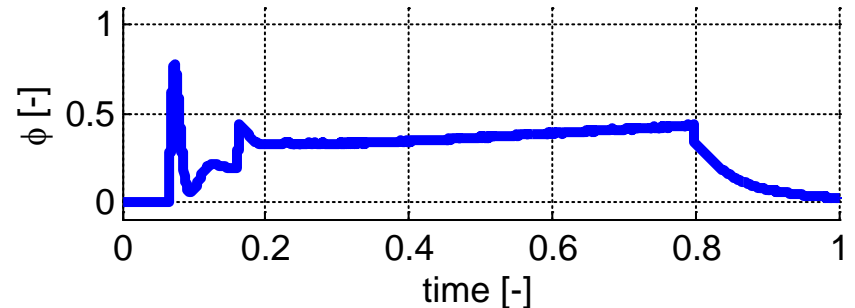
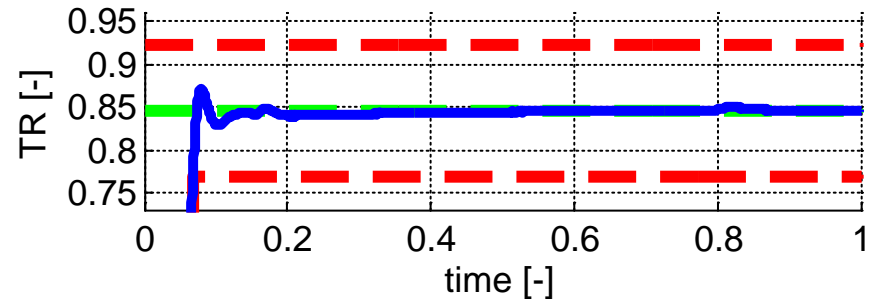


# Simulation (High reactivity)

## Automatic Monomer Feed (Product A)



## Constant Monomer Feed (Product B)

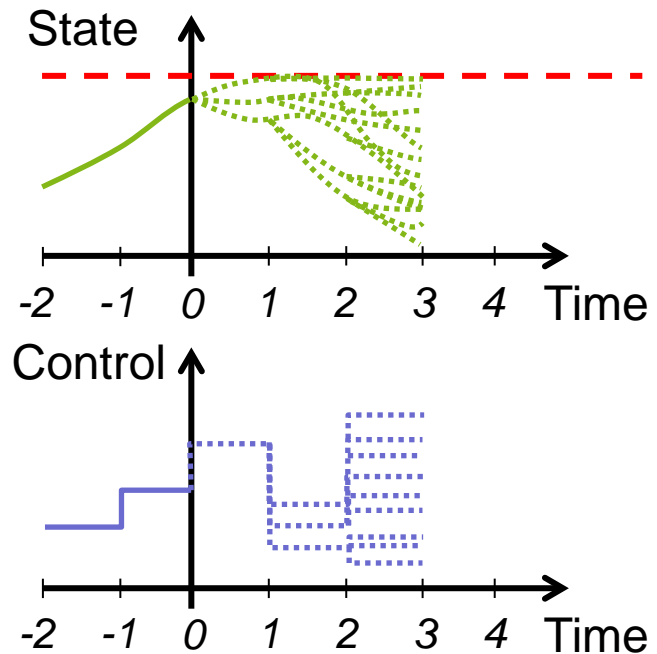
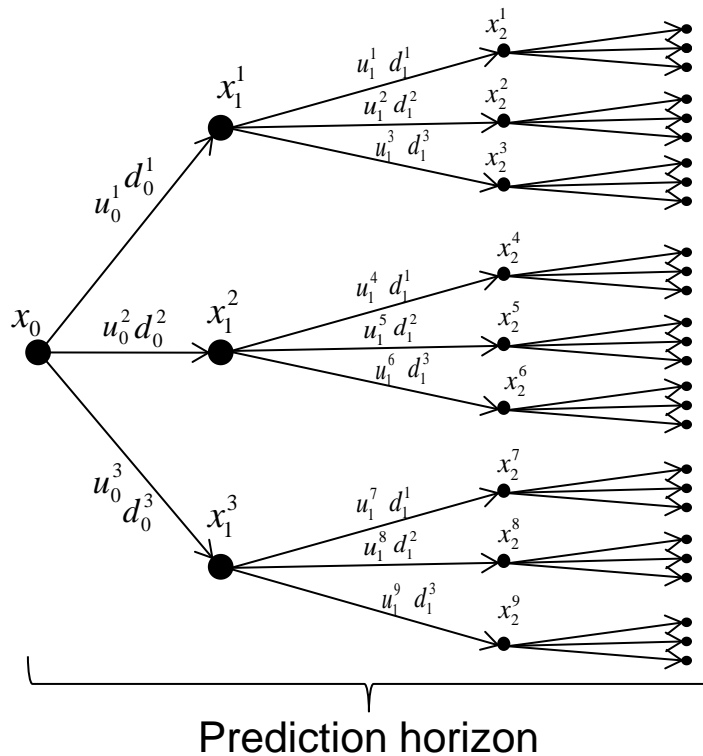


# Conclusions

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- Combined state and parameter estimation is feasible
  - **Constraint: At least as many independent measurements as unknown parameters are needed!**
- How can the robustness of the controller be improved or even guaranteed?

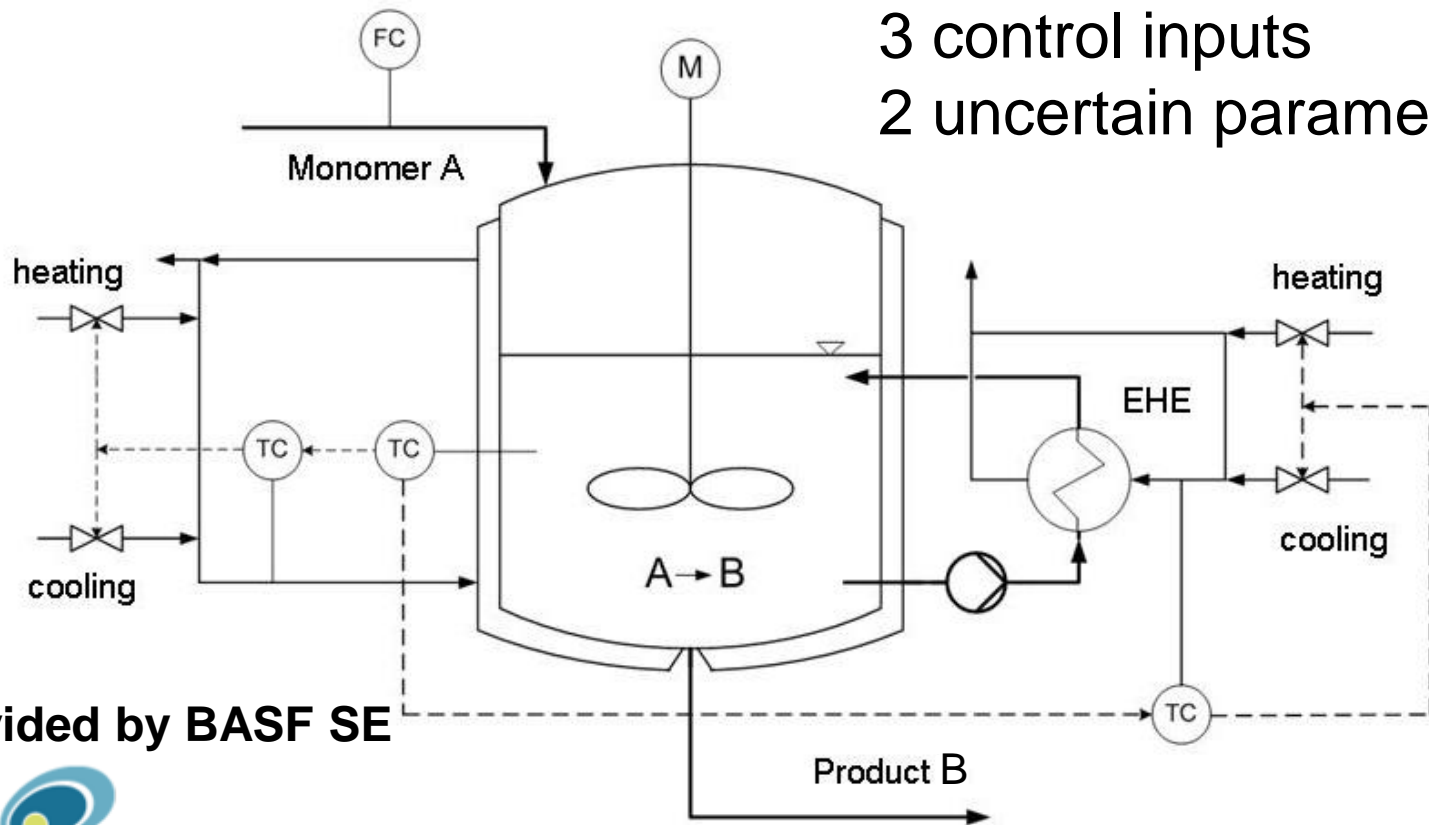
# Multi-stage NMPC: Formulation



- Uncertainty is modelled by a scenario tree
- Constraints must be met for all values of the uncertainty
- Controller will react to the information gained at the next stage
- This is taken into account in the optimization of the next decisions

# An industrial batch polymerization reactor control problem

8 differential states  
3 control inputs  
2 uncertain parameters



Model provided by BASF SE



[Lucia, Andersson, Brandt, Diehl & Engell, JPC, 2014]

# Formulation of the NMPC problem

- Control task:

- Minimize the batch time while satisfying temperature constraints for all the values of two uncertain ( $\pm 30\%$ ) parameters

- Standard NMPC with tracking cost:

$$J_{\text{track}} = \sum_{k=0}^{N_p-1} -m_{P,k}^j + q(T_{R,k}^j - T_{\text{set}})^2 + r \Delta u_k^j{}^2$$

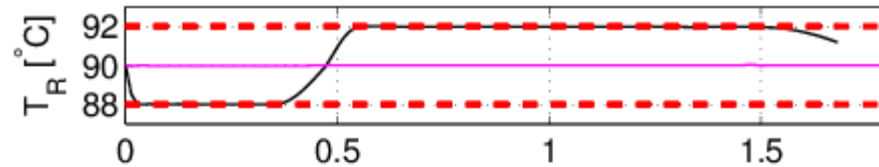
- Multi-stage NMPC with economic cost function:

$$J_{\text{eco}} = \sum_{i=1}^N \omega_i \sum_{k=0}^{N_p-1} -m_{P,k}^j + r \Delta u_k^j{}^2$$

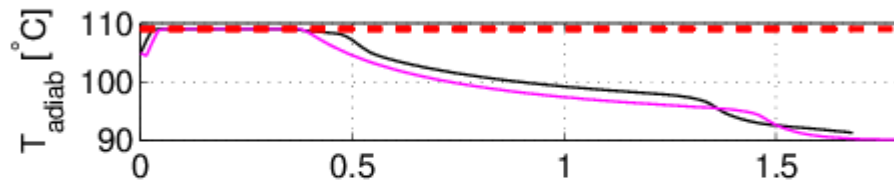
# Standard NMPC: No uncertainties

- Comparison of tracking and economic NMPC

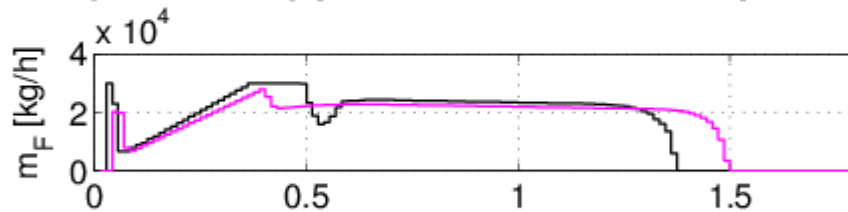
Reactor temperature



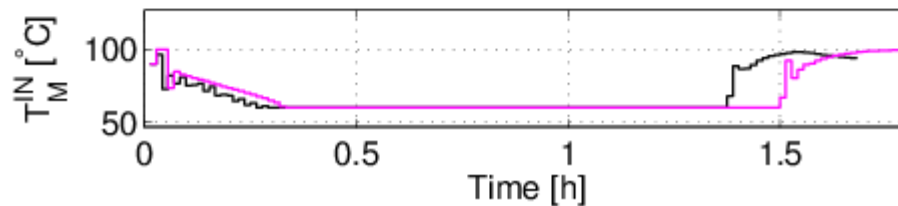
Adiabatic temperature



Monomer feed rate

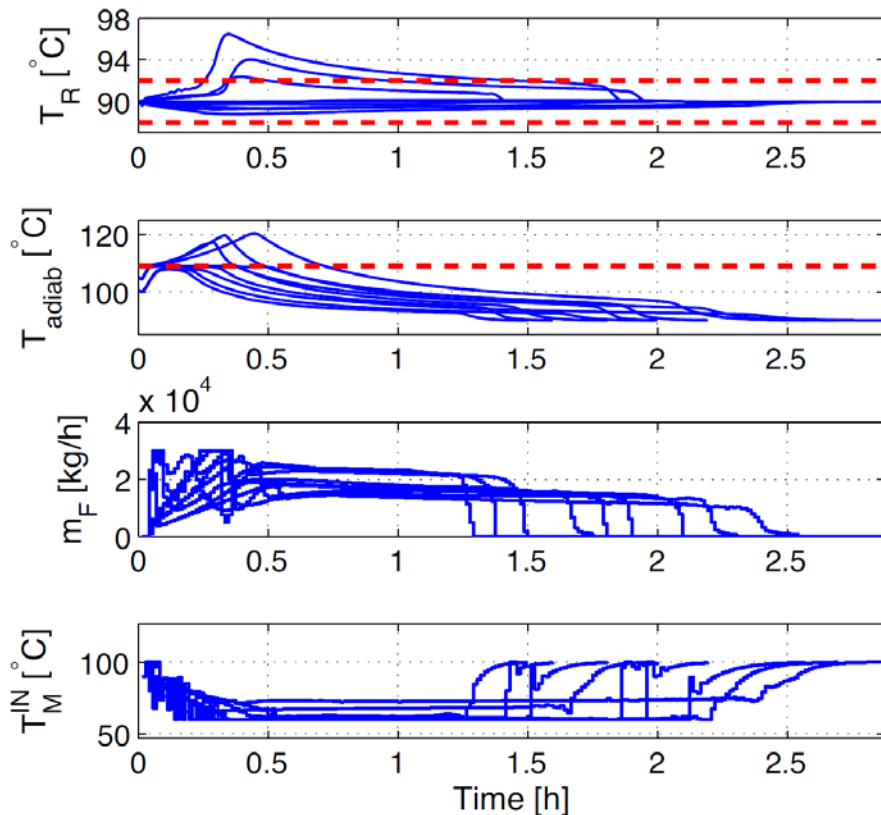


Jacket inlet temperature

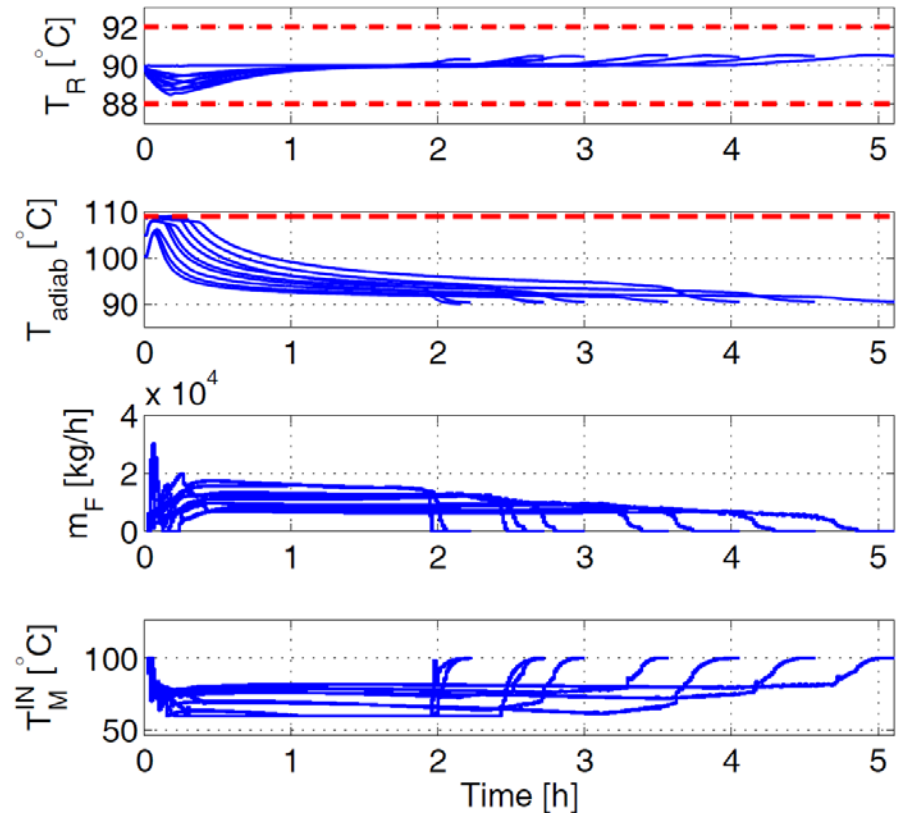


# Simulation results for different scenarios

## Standard NMPC



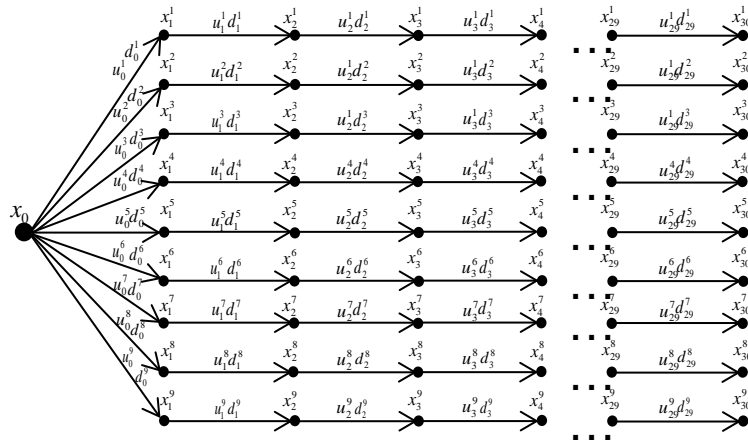
## Standard NMPC with conservative choice of parameters



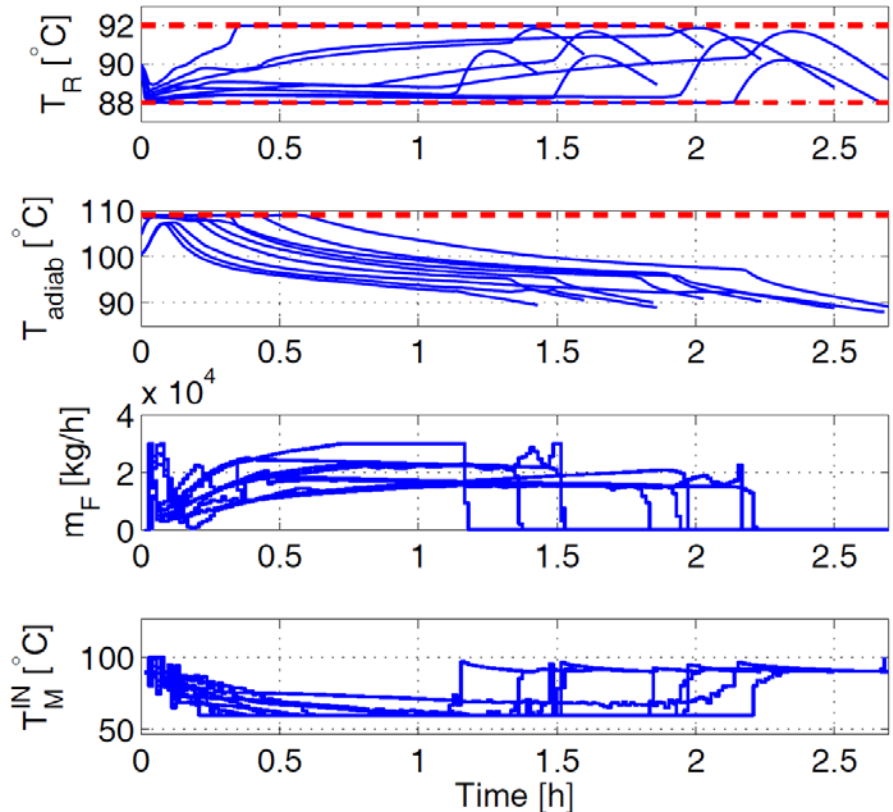
Simulations for different values of  $k$  and  $\Delta H$  ( $\pm 30\%$ )

# Simulation results for different scenarios

- Simple scenario tree
  - Extreme values of the uncertainty
  - Branch the tree only one stage



## Multi-stage NMPC



Simulations for different values of  $k$  and  $\Delta H$  ( $\pm 30\%$ )



# Comparison with standard NMPC

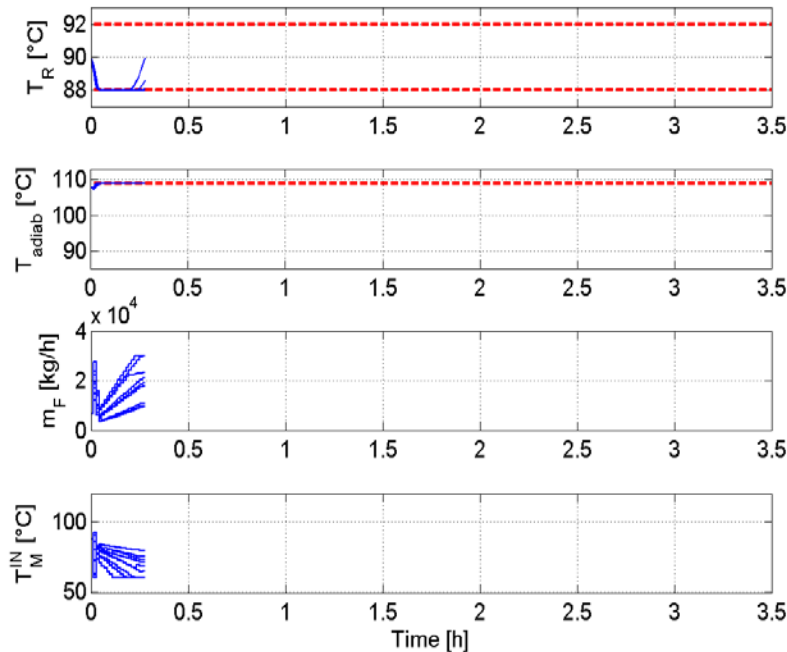
Scenario		Batch time in hours		
$\Delta H_R$	$k_0$	Standard NMPC	Standard (cons.)	Multi-stage
+30%	+30%	infeasible	2.15	2.03
+30%	0%	infeasible	2.72	2.24
+30%	-30%	infeasible	4.05	2.69
0%	+30%	1.60	2.22	1.60
0%	0%	1.81	3.00	1.84
0%	-30%	2.69	4.57	2.50
-30%	+30%	1.50	2.72	1.43
-30%	0%	1.99	3.57	1.86
-30%	-30%	2.88	5.11	2.68
Av. batch time [h]		infeasible	3.35	2.10

- Batch time reduction of 60% w.r.t. standard (cons.) NMPC

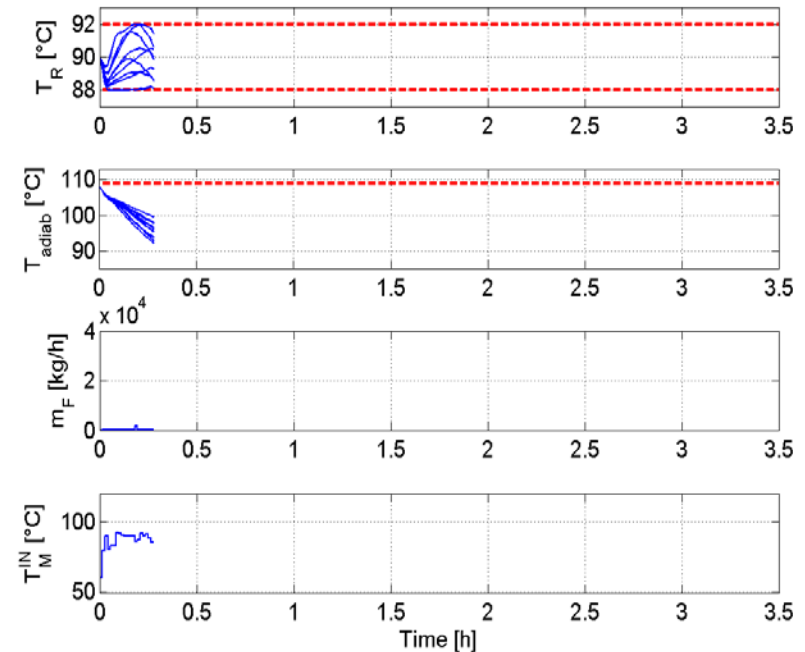
Comp time [s]	Standard NMPC	Standard (cons.)	Multi-stage
Average	0.072	0.059	1.134
Maximum	0.230	0.179	1.550

# Comparison with open-loop robust NMPC

## Multi-stage NMPC



## Open-loop robust NMPC ~ 25% longer batch!



# Multi-stage optimizing control - conclusions

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- The improvement of the robustness is very convincing.
- Direct solution without a need for specific engineering
- Improvement over nominal NMPC even when parameter updates are available
- Numerically tractable

# Summary

- Advanced control offers a significant potential for improved operations.
- **One can control well without an exact model!**
- Different solutions presented:
  - Tracking of optimality conditions – purely measurement based
  - Adaptation of a simplified prediction model
  - Multi-stage robust model-based optimization
- Modeling effort is the bottleneck in the solution of practical problems.
  - Robust formulations reduce the modeling effort
- **Unresolved problem:**  
Satisfaction of complex product property constraints
  - Direct measurements (e.g. Raman)
  - Soft sensors with additional online measurements - not necessarily selective, e.g. ultrasound, conductivity, pH, turbidity
  - But must be calibrated

# Copolymerization – Simulation study

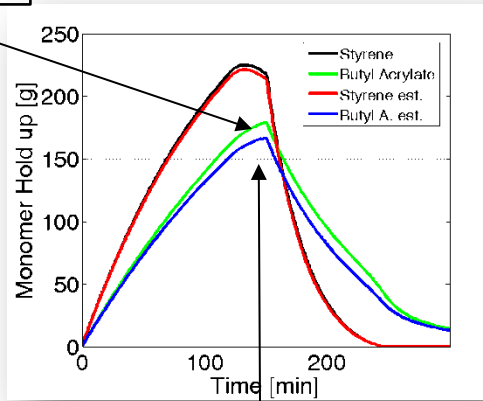
- Simulation study of a seeded semi-batch copolymerization
  - Industrial scale
  - Styrene and butyl acrylate
  - Seeded semi-batch process
  - Only temperature control
- Assuming a correct model that predicts the sound velocity
- Comparison of state estimator performances
  - Based on temperature measurements
  - Based on temperature and sound velocity measurements

# Copolymerization – Simulation Study

Mismatch in reactivity ratios (+/-10%)

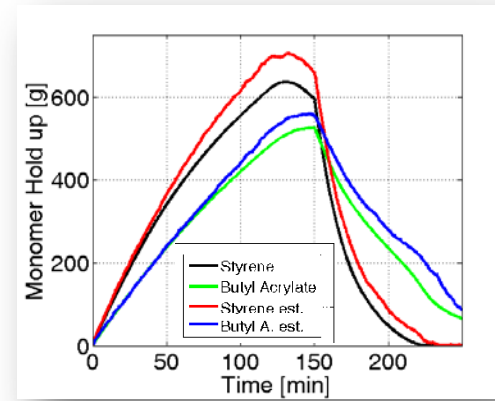
Maximum offset 6.5%

State estimator based on temperature

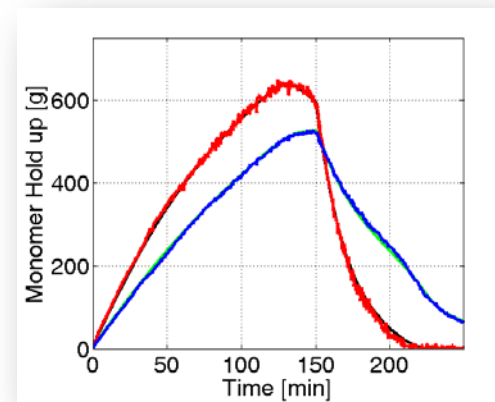
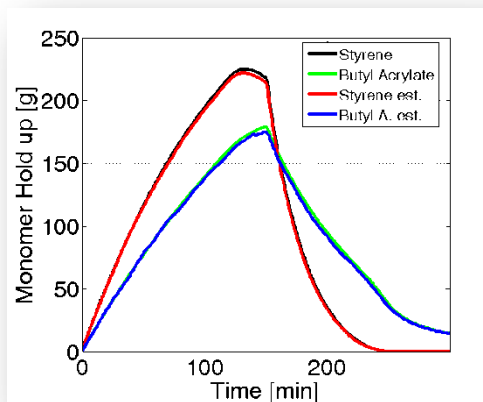


Feed stop

$kp_{11}$ -10%,  $kp_{22}$ +10%,  
 $\Delta H_{R,1}$ -10%,  $\Delta H_{R,2}$ +10%



State estimator based on temperature and sound velocity



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THANK YOU VERY MUCH FOR YOUR KIND ATTENTION!